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DESCRIPTION AND USAGE OF GENERAL BENDING

RESPONSE CODE 3 (GBRC3)

by

F. Henderson

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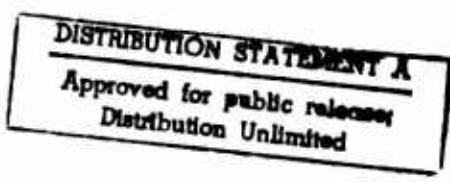


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ABSTRACT

The method of expanding General Bending Response Code 1 (GBRC1) to include the calculation of critical whirling frequencies and response of shafting systems is described. The extended computer program is designated General Bending Response Code 3 (GBRC3). Specifications for data, input forms and a practical application of the program are included.

ADMINISTRATIVE INFORMATION

The work reported here was carried out under Job Order number 1-823-343-01, Subproject SR 003 03 01, Task 10919.

I. INTRODUCTION

The method of analysis used in the development of General Bending Response Codes 1 and 2, references 2 and 3, Section II, is applied to the partial differential equations of motion for a whirling shaft as derived by Norman H. Jasper. Since the differential equations describe a coupling of flexural vibrations in two planes, the analysis results in a set of time-independent finite-difference equations in terms of deflections and moments occurring in these planes. General Bending Response Code 3 solves this system of difference equations for: (1) the response patterns of the shaft through a specified range of frequencies of the exciting forces and/or moments acting upon it, or (2) critical whirling frequencies and mode shapes of free vibration. The computed results consist of the components, absolute value, and phase angles of the vectors for deflection and moment in the two planes of shaft vibration.

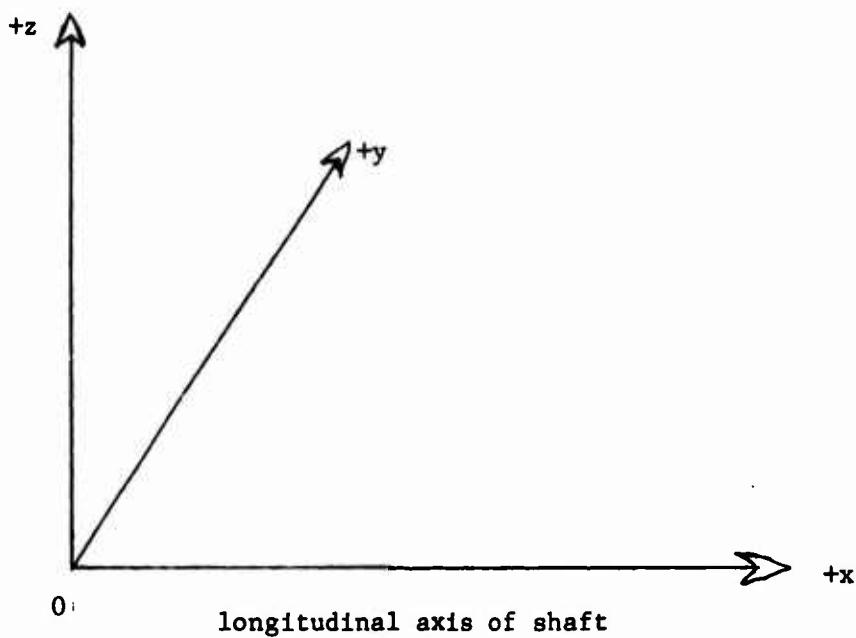
GBRC3 retains the provisions of previous codes in this series (references 2 and 3) for various types of damping and automatic calculation of frequency-dependent exciting forces and moments. Calculation of effective mass as a function of frequency is not included at this time. The code uses a FORTRAN IV compatible version of FORTRAN II and is currently being run with the IBSYS Operating System on the IBM 7090 computer at the Applied Mathematics Laboratory. An output tape for off-line plotting is written through use of the package of 7090 FORTRAN calling routines, AMPFOR, and the routine CXPLOT.

The facilities of GBRC3 along with GBRC1 and GBRC2 have been incorporated in a program package for ship vibration analysis, General Bending Response Program, which is in a testing stage.

II. ANALYSIS

The basic set of partial differential equations used for General Bending Response Code 3 were derived for a whirling shaft by Norman H. Jasper. The derivation is given in Section IV of reference 1. For the computer program, these equations were used in the form given in Section V of reference 1 and designated by [14].

As stated in reference 1, Section IV, the partial differential equations were derived for a shaft spinning with a uniform angular velocity, ω , about its longitudinal axis and having, simultaneously, a motion in two directions normal to the longitudinal shaft axis. The orientation of the shaft axis is shown below.



The set of partial differential equations for the whirling shaft is:

$$(2.1) \quad \frac{\partial V_y(x,t)}{\partial x} = -\mu(x) \frac{\partial^2 y(x,t)}{\partial t^2} - k_1(x) y(x,t) - c(x) \frac{\partial y(x,t)}{\partial t} + P_y(x,t)$$

$$(2.2) \quad \frac{\partial M_z(x,t)}{\partial x} = -V_y(x,t) - \tau(x)\omega \frac{\partial \alpha(x,t)}{\partial t} - \tau_d(x) \frac{\partial^2 \beta(x,t)}{\partial t^2} -$$

$$- k_\beta(x) \beta(x,t) + Q_z(x,t)$$

$$(2.3) \quad \frac{\partial \beta(x,t)}{\partial x} = - \frac{M_z(x,t)}{EI(x)}$$

$$(2.4) \quad \frac{\partial y(x,t)}{\partial x} = \beta(x,t) - \frac{V_y(x,t)}{KAG(x)}$$

$$(2.5) \quad \frac{\partial V_z(x,t)}{\partial x} = -\mu(x) \frac{\partial^2 z(x,t)}{\partial t^2} - k_1(x) z(x,t) - c(x) \frac{\partial z(x,t)}{\partial t} + P_z(x,t)$$

$$(2.6) \quad \frac{\partial M_y(x,t)}{\partial x} = -V_z(x,t) + \tau(x)\omega \frac{\partial \beta(x,t)}{\partial t} - \tau_d(x) \frac{\partial^2 \alpha(x,t)}{\partial t^2}$$

$$- k_\alpha(x) \alpha(x,t) + Q_y(x,t)$$

$$(2.7) \quad \frac{\partial \alpha(x,t)}{\partial x} = - \frac{M_y(x,t)}{EI(x)}$$

$$(2.8) \quad \frac{\partial z(x,t)}{\partial x} = \alpha(x,t) - \frac{V_z(x,t)}{KAG(x)}$$

Equations (2.1) through (2.4) are for the xy-plane and Equations (2.5) through (2.8) are for the xz-plane.

The notation for the equations is:

x	distance in the longitudinal direction measured from the origin of coordinates
t	time variable
y	displacement normal to x in the xy -plane of bending
z	displacement normal to x in the xz -plane of bending
α	slope of the projection of the normal to the shaft section in the xz -plane
β	slope of the projection of the normal to the shaft section in the xy -plane
v_y	shearing force in the direction of flexural vibration in the y -direction
v_z	shearing force in the direction of flexural vibration in the z -direction
M_z	bending moment relative to the z -axis
M_y	bending moment relative to the y -axis
μ	mass per unit length
τ_d	diametrical mass moment of inertia per unit length
KAG	shear rigidity
EI	bending rigidity
τ	polar mass moment of inertia per unit length
k_1	linear spring constant per unit length
k_8	rotatory spring constant per unit length acting in the xy -plane
k_a	rotatory spring constant per unit length acting in the xz -plane
c	damping coefficient
P_y	external force per unit length (excluding spring forces) in the y -direction
P_z	same as P_y except in the z -direction

Q_y external moment per unit length relative to the y-axis
 Q_z external moment per unit length relative to the z-axis
 ω angular spin velocity about the longitudinal axis of the shaft

The departure from Jasper's notation for shear rigidity, mass per unit length and external moments was made to preserve consistency with the GBRC series notation.

The viscous damping term does not appear in the basic differential equations in reference 1.

The partial differential equations (2.1) through (2.8) are transformed to a set of differential equations in terms of the natural angular whirling frequency, Ω , by making the substitution $\omega = h\Omega$ and assuming that all time-dependent quantities are simple harmonic functions of time. Then

$$\begin{aligned}
 M(x,t) &= M(x) e^{i\Omega t} & \alpha(x,t) &= \alpha(x)e^{i\Omega t} \\
 y(x,t) &= y(x) e^{i\Omega t} & \beta(x,t) &= \beta(x)e^{i\Omega t} \\
 (2.9) \quad V(x,t) &= V(x) e^{i\Omega t} & z(x,t) &= z(x)e^{i\Omega t} \\
 P(x,t) &= P(x) e^{i\Omega t} & Q(x,t) &= Q(x) e^{i\Omega t}.
 \end{aligned}$$

Substituting (2.9) into Equations (2.1) through (2.8) performing differentiations, and dividing out $e^{i\Omega t}$ gives the set of differential equations,

$$(2.10) \quad \frac{dV_y(x)}{dx} = \mu(x)\Omega^2 y(x) - [k_1(x)] y(x) - i\tau(x)h\Omega^2 c(x)y(x) + P_y(x)$$

$$(2.11) \quad \frac{dM_z(x)}{dx} = -V_y(x) - i\tau(x)h\Omega^2 a(x) + \tau_d(x)\Omega^2 \beta(x) - [k_\beta(x)] \beta(x) \\ + Q_z(x)$$

$$(2.12) \quad \frac{d\beta(x)}{dx} = -\frac{M_z(x)}{EI(x)}$$

$$(2.13) \quad \frac{dy(x)}{dx} = \beta(x) - \frac{V_y(x)}{KAG(x)}$$

$$(2.14) \quad \frac{dV_z(x)}{dx} = \mu(x)\Omega^2 z(x) - [k_1(x)] z(x) - i\tau(x)h\Omega^2 c(x)z(x) + P_z(x)$$

$$(2.15) \quad \frac{dM_y(x)}{dx} = -V_z(x) + i\tau(x)h\Omega^2 \beta(x) + \tau_d(x)\Omega^2 a(x) - [k_\alpha(x)] + Q_y(x)$$

$$(2.16) \quad \frac{da(x)}{dx} = -\frac{M_y(x)}{EI(x)}$$

$$(2.17) \quad \frac{dz(x)}{dx} = a(x) - \frac{V_z(x)}{KAG(x)}$$

Eliminating V_y between Equations (2.11) and (2.13) gives

$$(2.18) \quad \frac{dM_z(x)}{dx} - KAG(x) \frac{dy(x)}{dx} = -i\tau(x)h\Omega^2 a(x) + [\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x)] \cdot \\ \beta(x) + Q_z(x)$$

Eliminating V_z between Equations (2.15) and (2.17) gives

$$(2.19) \quad \frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} = [\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)] a(x) \\ + i\tau(x)h\Omega^2 \beta(x) + Q_y(x)$$

Solving Equations (2.18) and (2.19) for $\alpha(x)$ and $\beta(x)$,

$$\begin{aligned} \alpha(x) = & \left\{ -\frac{1}{\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x)} \left[\frac{dM_z(x)}{dx} - KAG(x) \frac{dy(x)}{dx} - Q_z(x) \right] \right. \\ & + \left. \frac{1}{i\tau(x)h\Omega^2} \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right] \right\} \frac{i\tau(x)h\Omega^2}{\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x)} \\ & + \left. \frac{\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)}{i\tau(x)h\Omega^2} \right\}^1 \end{aligned}$$

or

$$(2.20) \quad \alpha(x) = \frac{i\tau(x)h\Omega^2}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2}$$

$$\begin{aligned} & \left[-\frac{dM_z(x)}{dx} + KAG(x) \frac{dy(x)}{dx} + Q_z(x) \right] \\ & + \frac{\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x)}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2} \\ & \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right], \end{aligned}$$

and

$$\beta(x) = \left\{ -\frac{1}{i\tau(x)h\Omega^2} \left[KAG(x) \frac{dy(x)}{dx} - \frac{dM_z(x)}{dx} + Q_z(x) \right] \right.$$

$$+ \frac{1}{(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x))} \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right] \left. \right\}$$

$$\left\{ \frac{\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x)}{i\tau(x)h\Omega^2} + \frac{i\tau(x)h\Omega^2}{(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x))} \right\}^{-1}$$

or

$$(2.21) \quad \beta(x) = - \frac{(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x))}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2}$$

$$+ \frac{i\tau(x)h\Omega^2}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2}$$

$$\left[KAG(x) \frac{dy(x)}{dx} - \frac{dM_z(x)}{dx} + Q_z(x) \right]$$

$$+ \frac{i\tau(x)h\Omega^2}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2}$$

$$\left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right].$$

The expressions for $\alpha(x)$ and $\beta(x)$ can be easier written by defining;

$$E \equiv \frac{\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2}$$

$$B \equiv \frac{\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x)}{(\tau_d(x)\Omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\Omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\Omega^2)^2}$$

and

$$C = \frac{i\tau(x)h\omega^2}{(\tau_d(x)\omega^2 - KAG(x) - k_\beta(x))(\tau_d(x)\omega^2 - KAG(x) - k_\alpha(x)) - (\tau(x)h\omega^2)^2} .$$

Using these definitions, Equations (2.20) and (2.21) can be rewritten as

$$(2.22) \quad \alpha(x) = C \left[-\frac{dM_z(x)}{dx} + KAG(x) \frac{dy(x)}{dx} + Q_z(x) \right] +$$

$$B \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right]$$

$$(2.23) \quad \beta(x) = -E \left[KAG(x) \frac{dy(x)}{dx} - \frac{dM_z(x)}{dx} + Q_z(x) \right] +$$

$$C \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right] .$$

From Equation (2.13),

$$v_y(x) = -KAG(x) \left[\frac{dy(x)}{dx} - \beta(x) \right] .$$

Substituting (2.23) for $\beta(x)$

$$(2.24) \quad v_y(x) = -KAG(x) \left\{ \frac{dy(x)}{dx} + E \left[KAG(x) \frac{dy(x)}{dx} - \frac{dM_z(x)}{dx} + Q_z(x) \right] \right. \\ \left. - C \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right] \right\} .$$

From Equation (2.17),

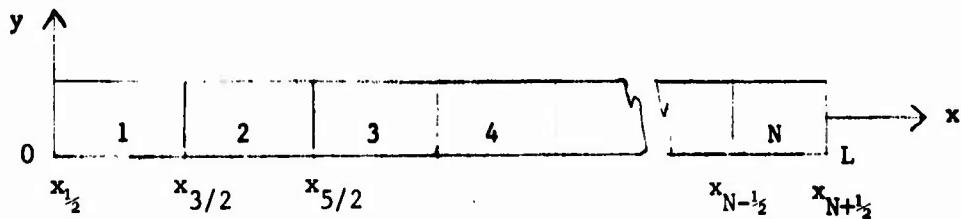
$$v_z(x) = KAG(x) \left[-\frac{dz(x)}{dx} + \alpha(x) \right] .$$

Substituting (2.22) for $\alpha(x)$,

$$(2.25) \quad v_z(x) = KAG(x) \left\{ -\frac{dz(x)}{dx} + C \left[-\frac{dM_z(x)}{dx} + KAG(x) \frac{dy(x)}{dx} + Q_z(x) \right] + B \left[\frac{dM_y(x)}{dx} - KAG(x) \frac{dz(x)}{dx} - Q_y(x) \right] \right\}.$$

The shaft interval from $x = 0$ to $x = L$ is subdivided by abscissas

$$x_{1/2} = 0 < x_{3/2} < x_{5/2} < \dots < x_{N+1/2} = L,$$



where L is the shaft length.

Equation (2.10) is then integrated from $x_{n-1/2}$ to $x_{n+1/2}$ for
 $n = 1, 2, 3, \dots, N$, giving

$$v_{y_{n+1/2}} - v_{y_{n-1/2}} = \int_{x_{n-1/2}}^{x_{n+1/2}} \left[\mu(x)\Omega^2 - (k_y)_n^2 - i\omega c_y(x) \right] y(x) dx + \int_{x_{n-1/2}}^{x_{n+1/2}} p_y(x) dx,$$

which can be approximated by

$$(2.26) \quad v_{y_{n+1/2}} - v_{y_{n-1/2}} = \left[(\mu\Delta x)_n \Omega^2 - (k_y)_n^2 - i(c_y \Delta x)_n \Omega \right] y_n + p_{y_n}$$

where

$$(\mu\Delta x)_n = \int_{x_{n-1/2}}^{x_{n+1/2}} \mu(x) dx$$

$$(k_y)_n = (k_1 \Delta x)_n = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} (k_1)_y dx$$

$$(c_y \Delta x) = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} c_y(x) dx$$

$$(P_y)_n = (P_y \Delta x)_n = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} P_y(x) dx$$

From Equation (2.24), $v_{y_{n+\frac{1}{2}}}$ is approximated for $n = 1, 2, 3, \dots, N-1$ by

$$(2.27) \quad v_{y_{n+\frac{1}{2}}} = - \left(\frac{KAG}{\Delta x} \right)_{n,n+1} \left\{ y_{n+1} - y_n + E_{n,n+1} \right.$$

$$\left[KAG_{n,n+1} (y_{n+1} - y_n) - (M_{z_{n+1}} - M_{z_n}) + Q_{z_{n,n+1}} \right]$$

$$\left. - C_{n,n+1} \left[M_{y_{n+1}} - M_{y_n} - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n,n+1}} \right] \right\},$$

where

$$\left(\frac{\Delta x}{KAG} \right)_{n,n+1} = \int_{x_n}^{x_{n+1}} \frac{dx}{KAG(x)}$$

$$Q_{z_{n,n+1}} = \int_{x_n}^{x_{n+1}} Q_z(x) dx$$

$$Q_{y_{n,n+1}} = \int_{x_n}^{x_{n+1}} Q_y(x) dx ,$$

$$E_{n,n+1} = \frac{\tau_{d_{n,n+1}} \Omega^2 - KAG_{n,n+1} - k_{\alpha_{n,n+1}}}{(\tau_{d_{n,n+1}} \Omega^2 - KAG_{n,n+1} - k_{\beta_{n,n+1}})(\tau_{d_{n,n+1}} \Omega^2 - KAG_{n,n+1} - k_{\alpha_{n,n+1}}) - (\tau_{n,n+1} h \Omega^2)^2}$$

$$C_{h,h+1} = \frac{i(\tau_{n,n+1} h \Omega^2)}{(\tau_{d_{n,n+1}} \Omega^2 - KAG_{n,n+1} - k_{\beta_{n,n+1}})(\tau_{d_{n,n+1}} \Omega^2 - KAG_{n,n+1} - k_{\alpha_{n,n+1}}) - (\tau_{n,n+1} h \Omega^2)^2}$$

with

$$(\tau_{d \Delta x})_{n,n+1} = \int_{x_n}^{x_{n+1}} \tau_d dx$$

$$(\tau \Delta x)_{n,n+1} = \int_{x_n}^{x_{n+1}} \tau dx$$

$$(k_{\alpha \Delta x})_{n,n+1} = \int_{x_n}^{x_{n+1}} k_{\alpha} dx$$

$$(k_{\beta \Delta x})_{n,n+1} = \int_{x_n}^{x_{n+1}} k_{\beta} dx$$

and

$$x_n = \frac{1}{2} (x_{n+\frac{1}{2}} + x_{n-\frac{1}{2}}) .$$

Substituting (2.27) into (2.26) gives

$$\begin{aligned}
 (2.28) \quad & -\left(\frac{KAG}{\Delta x}\right)_{n,n+1} \left\{ y_{n+1} - y_n + E_{n,n+1} \left[KAG_{n,n+1} (y_{n+1} - y_n) - \right. \right. \\
 & \quad \left. \left. (M_{z_{n+1}} - M_{z_n}) + Q_{z_{n,n+1}} \right] \right\} \\
 & - C_{n,n+1} \left[M_{y_{n+1}} - M_{y_n} - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n,n+1}} \right] \\
 & + \left(\frac{KAG}{\Delta x}\right)_{n-1,n} \left\{ y_n - y_{n-1} + E_{n-1,n} \left[KAG_{n-1,n} (y_n - y_{n-1}) - \right. \right. \\
 & \quad \left. \left. (M_{z_n} - M_{z_{n-1}}) + Q_{z_{n-1,n}} \right] \right\} \\
 & - C_{n-1,n} \left[M_{y_n} - M_{y_{n-1}} - KAG_{n-1,n} (z_n - z_{n-1}) - Q_{y_{n-1,n}} \right] \\
 & = \left[(\mu \Delta x)_n \Omega^2 - k_y - i(c_y \Delta x)_n \Omega \right] y_n + P_{y_n} ,
 \end{aligned}$$

for $n = 1, 2, \dots, N-1$.

Similarly, Equation (2.14) is integrated from $x_{n-\frac{1}{2}}$ to $x_{n+\frac{1}{2}}$ for $n = 1, 2, 3, \dots, N-1$ giving

$$\begin{aligned}
 v_{z_{n+\frac{1}{2}}} - v_{z_{n-\frac{1}{2}}} & = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} \left[\mu(x) \Omega^2 - (k_1)_z - i \Omega c_z(x) \right] z(x) dx \\
 & + \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} P_z(x) dx ,
 \end{aligned}$$

which is then approximated by

$$(2.29) \quad v_{z_{n+\frac{1}{2}}} - v_{z_{n-\frac{1}{2}}} = \left[(\mu \Delta x)_n \Omega^2 - (k_z)_n - i(c_z \Delta x)_n \Omega \right] z_n + p_{z_n},$$

where

$$(k_z)_n = (k_1 \Delta x)_n = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} (k_1)_z dx$$

$$(c_z \Delta x)_n = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} c_z(x) dx$$

and

$$p_{z_n} = (P_z \Delta x)_n = \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} P_z(x) dx.$$

From Equation (2.25), $v_{z_{n+\frac{1}{2}}}$ can be approximated for $n = 1, 2, 3, \dots, N-1$

by

$$(2.30) \quad v_{z_{n+\frac{1}{2}}} = \left(\frac{KAG}{\Delta x} \right)_{n,n+1} \left\{ -(z_{n+1} - z_n) + C_{n,n+1} \left[-(M_{z_{n+1}} - M_{z_n}) \right. \right. \\ \left. \left. + KAG_{n,n+1} (y_{n+1} - y_n) + Q_{z_{n,n+1}} \right] \right. \\ \left. + B_{n,n+1} \left[M_{y_{n+1}} - M_{y_n} - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n,n+1}} \right] \right\},$$

where

$$B_{n,n+1} = \frac{\tau_{d_{n,n+1}}^{2-KAG_{n,n+1}-k_{\beta_{n,n+1}}}}{(\tau_{d_{n,n+1}}^{2-KAG_{n,n+1}-k_{\beta_{n,n+1}}})(\tau_{d_{n,n+1}}^{2-KAG_{n,n+1}-k_{\alpha_{n,n+1}}}) - (\tau_{n,n+1}^{h\Omega^2})^2}$$

Substitution of (2.30) into (2.29) gives for $n = 1, 2, \dots, N-1$

$$(2.31) \quad \left(\frac{KAG}{\Delta x} \right)_{n,n+1} \left\{ -(z_{n+1} - z_n) + C_{n,n+1} \left[-(M_{z_{n+1}} - M_{z_n}) + KAG_{n,n+1} \right. \right.$$

$$\left. (y_{n+1} - y_n) + Q_{z_{n,n+1}} \right]$$

$$+ B_{n,n+1} \left[M_{y_{n+1}} - M_{y_n} - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n,n+1}} \right] \Big\}$$

$$- \left(\frac{KAG}{\Delta x} \right)_{n-1,n} \left\{ -(z_n - z_{n-1}) + C_{n-1,n} \left[-(M_{z_n} - M_{z_{n-1}}) + KAG_{n-1,n} \right. \right.$$

$$\left. (y_n - y_{n-1}) + Q_{z_{n-1,n}} \right]$$

$$+ B_{n-1,n} \left[M_{y_n} - M_{y_{n-1}} - KAG_{n-1,n} (z_n - z_{n-1}) - Q_{y_{n-1,n}} \right] \Big\}$$

$$= \left[(\mu \Delta x)_n^2 - k_{z_n} - i(c_z \Delta x)_n^2 \right] z_n + p_{z_n} .$$

Integrating Equation (2.16) from $x_{n-\frac{1}{2}}$ to $x_{n+\frac{1}{2}}$ for $n = 1, 2, \dots, N$,

$$a_{n+\frac{1}{2}} - a_{n-\frac{1}{2}} = - \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} \frac{M_y(x)}{EI(x)} dx ,$$

and approximating the integral on the right side gives

$$(2.32) \quad a_{n+1} - a_{n-1} = -\left(\frac{\Delta x}{EI}\right)_n M_y_n$$

where

$$\left(\frac{\Delta x}{EI}\right)_n = \int_{x_{n-1}}^{x_{n+1}} \frac{dx}{EI(x)} .$$

Approximate a_{n+1} for $n = 1, 2, \dots, N-1$ using (2.22),

$$(2.33) \quad a_{n+1} = \left(\frac{1}{\Delta x}\right)_{n,n+1} \left\{ C_{n,n+1} \left[-(M_{z_{n+1}} - M_{z_n}) + KAG_{n,n+1} (y_{n+1} - y_n) + Q_{z_{n,n+1}} \right] + B_{n,n+1} \left[(M_{y_{n+1}} - M_{y_n}) - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n,n+1}} \right] \right\} .$$

Substituting (2.33) into (2.32) gives for $n = 1, 2, \dots, N-1$

$$(2.34) \quad \begin{aligned} & \left(\frac{1}{\Delta x}\right)_{n,n+1} \left\{ C_{n,n+1} \left[-(M_{z_{n+1}} - M_{z_n}) + KAG_{n,n+1} (y_{n+1} - y_n) + Q_{z_{n,n+1}} \right] \right. \\ & \quad \left. + B_{n,n+1} \left[M_{y_{n+1}} - M_{y_n} - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n,n+1}} \right] \right\} \\ & - \left(\frac{1}{\Delta x}\right)_{n-1,n} \left\{ C_{n-1,n} \left[-(M_{z_n} - M_{z_{n-1}}) + KAG_{n-1,n} (y_n - y_{n-1}) + Q_{z_{n-1,n}} \right] \right. \\ & \quad \left. + B_{n-1,n} \left[M_{y_n} - M_{y_{n-1}} - KAG_{n-1,n} (z_n - z_{n-1}) - Q_{y_{n-1,n}} \right] \right\} \\ & = - \left(\frac{\Delta x}{EI}\right)_n M_y_n . \end{aligned}$$

Integrating Equation (2.12) from $x_{n-\frac{1}{2}}$ to $x_{n+\frac{1}{2}}$ for $n = 1, 2, \dots, N$,

$$\beta_{n+\frac{1}{2}} - \beta_{n-\frac{1}{2}} = - \int_{x_{n-\frac{1}{2}}}^{x_{n+\frac{1}{2}}} \frac{M_z(x)}{EI(x)} dx ,$$

and approximating the right side, one has

$$(2.35) \quad \beta_{n+\frac{1}{2}} - \beta_{n-\frac{1}{2}} = - \left(\frac{\Delta x}{EI} \right)_n M_{z_n} .$$

Approximating $\beta_{n+\frac{1}{2}}$ with (2.23) for $n = 1, 2, \dots, N$,

$$(2.36) \quad \beta_{n+\frac{1}{2}} = - \left(\frac{1}{\Delta x} \right)_{n,n+1} \left\{ E_{n,n+1} \left[KAG_{n,n+1} (y_{n+1} - y_n) - (M_{z_{n+1}} - M_z) + Q_{z_{n+1}} \right] \right. \\ \left. - C_{n,n+1} \left[M_{y_{n+1}} - M_{y_n} - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n+1}} \right] \right\},$$

and substituting into (2.35) gives for $n = 1, 2, \dots, N-1$,

$$(2.37) \quad - \left(\frac{1}{\Delta x} \right)_{n,n+1} \left\{ E_{n,n+1} \left[KAG_{n,n+1} (y_{n+1} - y_n) - (M_{z_{n+1}} - M_z) + Q_{z_{n+1}} \right] \right. \\ \left. - C_{n,n+1} \left[(M_{y_{n+1}} - M_{y_n}) - KAG_{n,n+1} (z_{n+1} - z_n) - Q_{y_{n+1}} \right] \right\} \\ + \left(\frac{1}{\Delta x} \right)_{n-1,n} \left\{ E_{n-1,n} \left[KAG_{n-1,n} (y_n - y_{n-1}) - (M_{z_n} - M_{z_{n-1}}) + Q_{z_{n-1,n}} \right] \right. \\ \left. - C_{n-1,n} \left[(M_{y_n} - M_{y_{n-1}}) - KAG_{n-1,n} (z_n - z_{n-1}) - Q_{y_{n-1,n}} \right] \right\} \\ = - \left(\frac{\Delta x}{EI} \right)_n M_{z_n} .$$

End Conditions. The conditions required at the ends of the shaft determine the values of

$$v_{y_1}, v_{z_1}, \alpha_1, \beta_1, \text{ and } v_{y_{N+1}}, v_{z_{N+1}}, \alpha_{N+1}, \text{ and } \beta_{N+1}.$$

For free ends, the values imposed on V are

$$(2.38) \quad \begin{aligned} v_{y_1} &= v_{z_1} = 0 \quad \text{for } v_y(0) = v_z(0) = 0 \\ &\text{and} \end{aligned}$$

$$v_{y_{N+1}} = v_{z_{N+1}} = 0 \quad \text{for } v_y(L) = v_z(L) = 0.$$

Since for a free end both shear and moment are 0, the following values are assigned to M,

$$(2.39) \quad \begin{aligned} M_{y_1} &= M_{z_1} = 0 \\ &\text{and} \end{aligned}$$

$$M_{y_L} = M_{z_L} = 0.$$

If, on the other hand, the ends are fixed the conditions imposed on α and β are

$$(2.40) \quad \begin{aligned} \alpha_1 &= \beta_1 = 0 \quad \text{for } \alpha(0) = \beta(0) = 0 \\ &\text{and} \\ \alpha_{N+1} &= \beta_{N+1} = 0 \quad \text{for } \alpha(L) = \beta(L) = 0. \end{aligned}$$

In addition the values for y and z at the fixed end are

$$(2.41) \quad \begin{aligned} y_1 &= z_1 = 0 \quad \text{for } y(0) = z(0) = 0 \\ &\text{and} \\ y_N &= z_N = 0 \quad \text{for } y(L) = z(L) = 0. \end{aligned}$$

To arrange Equations (2.28), (2.31), (2.34) and (2.37) in a convenient form for solution the following is done:

a) Redefine $E_{n,n+1}$, $B_{n,n+1}$ and $C_{n,n+1}$,

$$E_{n,n+1} = \left(\frac{1}{\Delta x}\right)_{n,n+1} E_{n,n+1}$$

$$B_{n,n+1} = \left(\frac{1}{\Delta x}\right)_{n,n+1} B_{n,n+1}$$

$$C_{n,n+1} = \left(\frac{1}{\Delta x}\right)_{n,n+1} C_{n,n+1}$$

and

$$E'_{n,n+1} = KAG_{n,n+1} \cdot E_{n,n+1}$$

$$B'_{n,n+1} = KAG_{n,n+1} \cdot B_{n,n+1}$$

$$C'_{n,n+1} = KAG_{n,n+1} \cdot C_{n,n+1}$$

$$E''_{n,n+1} = KAG_{n,n+1}^2 \cdot E_{n,n+1}$$

$$B''_{n,n+1} = KAG_{n,n+1}^2 \cdot B_{n,n+1}$$

$$C''_{n,n+1} = KAG_{n,n+1}^2 \cdot C_{n,n+1}$$

$$L_{n,n+1} = \left(\frac{\Delta x}{KAG}\right)_{n,n+1}^{-1}$$

$$\zeta_n = \left(\frac{\Delta x}{EI}\right)_n$$

$$\delta'_{y_n} = \left[(u \Delta x)_n \Omega^2 - (k_y \Delta x)_n - i(c_y \Delta x)_n \Omega \right]$$

$$\delta'_{z_n} = \left[(u \Delta x)_n \Omega^2 - (l_z \Delta x)_n - i(c_z \Delta x)_n \Omega \right].$$

b) Multiply Equations (2.28) and (2.34) by -1.

With a) and b) the final system of equations is, after collecting terms for the coefficients,

$$\begin{aligned}
 (2.42) \quad & (L_{n-1,n} + E''_{n-1,n}) y_{n-1} - E'_{n-1,n} M_{z_{n-1}} + C''_{n-1,n} z_{n-1} - C'_{n-1,n} M_{y_{n-1}} \\
 & - (L_{n-1,n} + L_{n,n+1} + E''_{n-1,n} + E''_{n,n+1} - \delta'_y) y_n + (E'_{n-1,n} + E'_{n,n+1}) M_{z_n} \\
 & - (C''_{n-1,n} + C''_{n,n+1}) z_n \\
 & + (C'_{n-1,n} + C'_{n,n+1}) M_{y_n} + (L_{n,n+1} + E''_{n,n+1}) y_{n+1} - E'_{n,n+1} M_{z_{n+1}} \\
 & + C''_{n,n+1} z_{n+1} - C'_{n,n+1} M_{y_{n+1}} \\
 = & E'_{n-1,n} Q_{z_{n-1,n}} - E'_{n,n+1} Q_{z_{n,n+1}} + C'_{n-1,n} Q_{y_{n-1,n}} - C'_{n,n+1} Q_{y_{n,n+1}} - p_{y_n}
 \end{aligned}$$

$$\begin{aligned}
 (2.43) \quad & -E'_{n-1,n} y_{n-1} + E_{n-1,n} M_{z_{n-1}} - C'_{n-1,n} z_{n-1} + C_{n-1,n} M_{y_{n-1}} \\
 & + (E'_{n-1,n} + E'_{n,n+1}) y_n \\
 & - (E_{n-1,n} + E_{n,n+1} - \zeta_n) M_{z_n} + (C'_{n-1,n} + C'_{n,n+1}) z_n - (C_{n-1,n} + C_{n,n+1}) M_{y_n} \\
 & - E'_{n,n+1} y_{n+1} + E_{n,n+1} M_{z_{n+1}} - C'_{n,n+1} z_{n+1} + C_{n,n+1} M_{y_{n+1}} \\
 = & - E_{n-1,n} Q_{z_{n-1,n}} + E_{n,n+1} Q_{z_{n,n+1}} - C_{n-1,n} Q_{y_{n-1,n}} + C_{n,n+1} Q_{y_{n,n+1}}
 \end{aligned}$$

$$\begin{aligned}
(2.44) \quad & C_{n-1,n}'' y_{n-1} - C_{n-1,n}' M_{z_{n-1}} - (L_{n-1,n} + B_{n-1,n}'') z_{n-1} + B_{n-1,n}' M_{y_{n-1}} \\
& - (C_{n-1,n}'' + C_{n,n+1}'') y_n \\
& + (C_{n-1,n}' + C_{n,n+1}') M_{z_n} + (L_{n-1,n} + L_{n,n+1} + B_{n-1,n}'' + B_{n,n+1}'' - \delta_z') z_n \\
& - (B_{n-1,n}' + B_{n,n+1}') M_{y_n} + C_{n,n+1}'' y_{n+1} - C_{n,n+1}' M_{z_{n+1}} - (L_{n,n+1} + B_{n,n+1}'') z_{n+1} \\
& + B_{n,n+1}' M_{y_{n+1}} \\
= & C_{n-1,n}' Q_{z_{n-1,n}} - C_{n,n+1}' Q_{z_{n,n+1}} - B_{n-1,n}' Q_{y_{n-1,n}} + B_{n,n+1}' Q_{y_{n,n+1}} + P_{z_n}
\end{aligned}$$

$$\begin{aligned}
(2.45) \quad & - C_{n-1,n}' y_{n-1} + C_{n-1,n} M_{z_{n-1}} + B_{n-1,n}' z_{n-1} - B_{n-1,n}' M_{y_{n-1}} \\
& + (C_{n-1,n}' + C_{n,n+1}') y_n - (C_{n-1,n}' + C_{n,n+1}') M_{z_n} \\
& - (B_{n-1,n}' + B_{n,n+1}') z_n + (B_{n-1,n}' + B_{n,n+1}' - \zeta_n) M_{y_n} - C_{n,n+1}' y_{n+1} \\
& + C_{n,n+1}' M_{z_{n+1}} + B_{n,n+1}' z_{n+1} - B_{n,n+1}' M_{y_{n+1}} \\
= & - C_{n-1,n}' Q_{z_{n-1,n}} + C_{n,n+1}' Q_{z_{n,n+1}} + B_{n-1,n}' Q_{y_{n-1,n}} - B_{n,n+1}' Q_{y_{n,n+1}}
\end{aligned}$$

These equations come respectively from Equations (2.28), (2.37), (2.31) and (2.34). For $n = 1$ and $n = N$, the end conditions as specified by the data will be included in the system of equations.

The matrix formulation of Equations (2.42) through (2.45) is

$$(2.46) \quad \vec{Az} = \vec{P}$$

as indicated in (2.20), (2.21) and (2.22) of reference 2 with the following definitions for the subvectors \vec{z}_n of \vec{z} and \vec{P}_n of \vec{P} , and the submatrices $A_{i,j}$ of the matrix A:

$$(2.47)$$

$$\vec{z}_n = \begin{vmatrix} y_n \\ M z_n \\ z_n \\ M y_n \end{vmatrix}, \quad \vec{P}_n = \begin{vmatrix} \tilde{P}_n \\ \tilde{P}'_n \\ \tilde{P}''_n \\ \tilde{P}'''_n \end{vmatrix}$$

$$\text{with } \tilde{P}_n = -P_{y_n} + E'_{n-1,n} Q_{z_{n-1,n}} - E'_{n,n+1} Q_{z_{n,n+1}} + C'_{n-1,n} Q_{y_{n-1,n}}$$

$$- C'_{n,n+1} Q_{y_{n,n+1}}$$

$$\tilde{P}'_n = -E_{n-1,n} Q_{z_{n-1,n}} + E_{n,n+1} Q_{z_{n,n+1}} - C_{n-1,n} Q_{y_{n-1,n}}$$

$$+ C_{n,n+1} Q_{y_{n,n+1}}$$

$$\tilde{P}''_n = P_{z_n} + C'_{n-1,n} Q_{z_{n-1,n}} - C'_{n,n+1} Q_{z_{n,n+1}} - B'_{n-1,n} Q_{y_{n-1,n}}$$

$$+ B'_{n,n+1} Q_{y_{n,n+1}}$$

$$\tilde{P}'''_n = -C_{n-1,n} Q_{z_{n-1,n}} + C_{n,n+1} Q_{z_{n,n+1}} + B_{n-1,n} Q_{y_{n-1,n}}$$

$$- B_{n,n+1} Q_{y_{n,n+1}},$$

and for $n = 2, 3, \dots, N-1$.

and for $n = 1$ and $n = N$,

$$A_{1,1} = \begin{vmatrix} (L_{1,2} + E'_{1,2} - \delta'_{y_1}) & E'_{1,2} & -C'_{1,2} \\ E'_{1,2} & -(E_{1,2} - \zeta_1) & C'_{1,2} \\ -C'_{1,2} & C'_{1,2} & (L_{1,2} + B'_{1,2} - \delta'_{z_1}) \\ C'_{1,2} & -C_{1,2} & -B'_{1,2} \\ C'_{1,2} & -B'_{1,2} & (B_{1,2} - \zeta_1) \end{vmatrix}$$

$$A_{N,N} = \begin{vmatrix} -(L_{N-1,N} + E'_{N-1,N} - \delta'_{y_N}) & E'_{N-1,N} & -C'_{N-1,N} \\ E'_{N-1,N} & -(E_{N-1,N} - \zeta_N) & C'_{N-1,N} \\ -C'_{N-1,N} & C'_{N-1,N} & (L_{N-1,N} + B_{N-1,N} - \delta'_{z_N}) \\ C'_{N-1,N} & -C_{N-1,N} & -B'_{N-1,N} \\ C'_{N-1,N} & -B'_{N-1,N} & (B_{N-1,N} - \zeta_N) \end{vmatrix}$$

If the ends are free, ζ_1 and ζ_N are chosen sufficiently large that M_1 and M_N become zero for practical purposes. If the ends are fixed, the condition above on moment is released and a sufficiently large value is given to k_{y_1} , k_{z_1} and k_{y_N} , k_{z_N} in the expressions

$$\delta'_{y_1} = \left[(\mu\Delta x)_1 \Omega^2 - k_{y_1} - i c_{y_1} \Omega \right],$$

$$\delta'_{z_1} = \left[(\mu\Delta x)_1 - k_{z_1} - i c_{z_1} \Omega \right] \quad \text{and}$$

$$\delta'_{y_N} = \left[(\mu\Delta x)_N \Omega^2 - k_{y_N} - i c_{y_N} \Omega \right],$$

$$\delta'_{z_N} = \left[(\mu\Delta x)_N - k_{z_N} - i c_{z_N} \Omega \right] \text{ so that } y_1, z_1 \text{ and } y_N, z_N$$

are similarly forced close to 0.

The generalization of this matrix formulation to include more than one shaft coupled elastically proceeds in the way described on pages 10-12 of reference 2. The submatrices $A_{n,m}$ of the generalized A-matrix are set up according to the various types of elastic connections allowed between sections of the shaft(s). If a section numbered n is connected rigidly to a section numbered m the submatrix generated is

$$A_{n,m} = \begin{vmatrix} (L_{n,m} + E'_{n,m}) & -E'_{n,m} & C'_{n,m} & -C'_{n,m} \\ -E'_{n,m} & E'_{n,m} & -C'_{n,m} & C'_{n,m} \\ C'_{n,m} & -C'_{n,m} & -(L_{n,m} + B'_{n,m}) & B'_{n,m} \\ -C'_{n,m} & C'_{n,m} & B'_{n,m} & -B'_{n,m} \end{vmatrix} .$$

For a spring connection between sections n and m, one has,

$$A_{n,m} = \begin{vmatrix} (k_y)_{n,m} + i\Omega(c_y)_{n,m} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -(k_z)_{n,m} - i\Omega(c_z)_{n,m} & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix},$$

where $(k_y)_{n,m}$ and $(k_z)_{n,m}$ are spring constants in the y and z directions respectively and $(c_y)_{n,m}$ and $(c_z)_{n,m}$ are the associated damping coefficients.

The diagonal submatrices are given by

$$A_{n,n} = -\sum_{\substack{m=1 \\ m \neq n}}^N A_{n,m} + D_n,$$

with

$$D_n = \begin{vmatrix} \delta'_y_n & 0 & 0 & 0 \\ 0 & \zeta_n & 0 & 0 \\ 0 & 0 & -\delta'_z_n & 0 \\ 0 & 0 & 0 & -\zeta_n \end{vmatrix}.$$

When a section n is connected through a spring to ground, one adds

to $A_{n,n}$,

$$\begin{vmatrix} -(k_y)_n - i(c_y)_n \Omega & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & (k_z)_n + i(c_z)_n \Omega & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

where $(k_y)_n$ and $(k_z)_n$ are the spring constants for the connection and $(c_y)_n$ and $(c_z)_n$ are the associated damping coefficients.

III. Input Preparation and Definition of Parameters

The parameters which are specified for whirling calculations with GBRC3 are:

$$(\mu \Delta x)_n$$

$$\left(\frac{\Delta x}{EI} \right)_n$$

$$(\Delta x)_{\frac{n,n+1}{n,m}}$$

$$\left(\frac{\Delta x}{KAG} \right)_{\frac{n,n+1}{n,m}}$$

$$(P_n)_y$$

$$(Q_{n,m})_y$$

$$(k_{n,m})_y$$

$$(c_{n,m})_y$$

$$(c_{n,m}/\Omega)_y$$

$$(P_n)_z$$

$$(Q_{n,m})_z$$

$$(k_{n,m})_z$$

$$(c_{n,m})_z$$

$$(c_{n,m}/\Omega)_z$$

$$(\tau_d \Delta x)_{\frac{n,n+1}{n,m}}$$

$$(\tau \Delta x)_{\frac{n,n+1}{n,m}}$$

$$(k_a \Delta x)_{\frac{n,n+1}{n,m}}$$

$$(k_b \Delta x)_{\frac{n,n+1}{n,m}}$$

h

Ω ,

where μ , EI, KAG, P_y , Q_y , k_y , c, τ_d , τ , k_a and k_b are defined on pages and and h and Ω are defined on page . The subscripts n, n+1 or n, m show how a parameter is located in the system of divided shafts. For example, $\frac{n,n+1}{n,m}$ means an averaging of the parameter or its reciprocal over the shaft interval extending from the midpoint of section numbered n to the midpoint of the section numbered $\frac{n+1}{m}$. A single subscript n means that the parameter or its reciprocal is averaged over the interval of the shaft section numbered n. This location of parameters is consistent with that given in Appendix 2 of reference 1. Also included as data are the total number of shaft sections, section numbers, system numbers associated with sections and connections, end-condition designators, frequency range with an interval which can be used for response or natural frequency calculations, parameter scaling factors and various options provided by the program.

To accommodate the additional parameters required for the sections and special connections, the input forms used with GBRC1 (vibrations in one plane) are augmented to include formats for continuation cards

which go with the basic data card types "41", "42," "43," "51," "52" and "53" described in Section IV of reference 2. The revised forms are shown in Section IV of this report.

The complete set of data card types to be used with GBRC3 is (cf. reference 2, Section IV):

1) Run Title Card

<u>Columns</u>	<u>Contents</u>
7 - 12	(62 H ΔΔ
13 - 72	Whatever title is to be associated with the run

2) Data Control Card

<u>Columns</u>	<u>Contents</u>
3 - 4 (Data card "type" is always designated by digits in these columns)	90
5 - 6]	Columns 5, 6 contain number of data cards <u>not</u> counting continuation cards, of type given by columns 7, 8 which follow for this case.
7 - 8]	
9 - 10]	Similar to previous four columns for next and each succeeding set of data cards of a particular type in the data deck.
11 - 12] etc.	

3) Case Title Card

<u>Columns</u>	<u>Contents</u>
3 - 4	10
7 - 12	(62 H ΔΔ
13 - 72	Case title

4) Option Control Card

<u>Columns</u>	<u>Contents</u>
3 - 4	20
9 - 12	Op 1: Added mass option selector. 0 for whirling calculations.
13 - 16	Op 2: Selector for A-matrix and P-vector setup option. <u>0002</u> for whirling calculations.
17 - 20	Op 3: Selector for edit routine to be used at each frequency. 0 for present.
21 - 24	Op 4: Selector for plotting. <u>0001</u> Plots of the edited tables for each frequency are required. <u>0002</u> Plot of the summary edit is required. <u>0003</u> Both types of plots as given above are required.
25 - 28	Op 5: Selector for A-matrix routine. 0 if A-matrix is not printed. <u>0001</u> if A-matrix is to be printed.
29 - 32	Op 6: # 0, Plot displacements and/or moments versus sections for each frequency. 0 - No plot. <u>0001</u> - Plot displacements only. <u>0002</u> - Plot moments only. <u>0003</u> - Plot displacements and moments.
33 - 36	Op 7: # 0, Plot displacements and/or moments versus frequency for selected sections. 0 <u>0001</u> <u>0002</u> Same designation as above. <u>0003</u>

<u>Columns</u>	<u>Contents</u>
41 - 44	Op 9: Selector to determine if forcing function is to be multiplied by Ω^2 (in radians). 0 - Force not multiplied. <u>0001</u> - Force is multiplied.
45 - 48	Op 10: Selector for natural frequency search. 0 - Forced response is obtained for all frequencies specified. <u>0001</u> - Natural frequencies and mode shapes are calculated.

5) Edit Control Card

<u>Columns</u>	<u>Contents</u>
3 - 4	21
9 - 12	
13 - 16	
17 - 20	
21 - 24	
25 - 28	Section numbers for those sections for which displacements and moments are to be tabulated versus frequency (summary edit).

6) General Data Card

<u>Columns</u>	<u>Contents</u>
3 - 4	30
7 - 8	Number of sections; maximum of 40 allowed with present version of GBRG3.
9 - 16	Starting frequency (Ω_1) in cps.
17 - 24	Upper limit for frequency (Ω_2) in cps.
25 - 32	Frequency interval ($\Delta\Omega$) in cps. Used as the increment for frequency either in a response calculation or a natural frequency search over the range specified by Ω_1 and Ω_2 above.
33 - 40	h, ratio of spinning frequency to whirling frequency

7) Section Parameter Cards

<u>Columns</u>	<u>Contents</u>
3 - 4	43
7 - 8	Section number
12	End condition - normally 0
	<u>Free end</u> for section n, 1 for $V_y(n) = M_z(n) = 0$
	and $V_z(n) = M_y(n) = 0$
	<u>Fixed end</u> for section n, 2 for $a(n) = \beta(n) = 0$
	and $y(n) = z(n) = 0$
15 - 16	System number
17 - 24	Mass of the section
25 - 32	Water inertia
33 - 40	$(\Delta x/EI)_n$
41 - 48	$(\Delta x)_{n,n+1}$
49 - 56	$(\Delta x/KAG)_{n,n+1}$
57 - 64	$(\tau_d \Delta x)_{n,n+1}$
	Program notation, TAUD • Δx
65 - 72	$(P_n)_y$

8) Section Parameter Cards (Continuation)

<u>Columns</u>	<u>Contents</u>
1 - 16	Blank
17 - 24	$(\tau \Delta x)_{n,n+1}$
	Program notation, TAU • Δx

<u>Columns</u>	<u>Contents</u>
25 - 32	$(k_{\alpha} \Delta x)_{n, n+1}$ Program notation, KA • Δx
33 - 40	$(k_{\beta} \Delta x)_{n, n+1}$ Program notation, KB • Δx
41 - 48	$(P_n)_z$

9) Scaling Factor Cards for Section Parameters

<u>Columns</u>	<u>Contents</u>
3 - 4	<u>41</u> if this card contains real parts of scaling factors. <u>42</u> if this card contains the imaginary parts of the scaling factors.
15 - 16	System number for which scaling factors on this card are to be applied.
17 - 72	Scaling factor for each parameter is given in those columns containing that parameter value on the section para- meter cards.

10) Scaling Factor Cards for Section Parameters (Continuation)

<u>Columns</u>	<u>Contents</u>
1 - 16	Blank
17 - 48	Scaling factor for each parameter given in those columns containing that parameter value on the continuation cards associated with the section parameter cards.

11) Special Connection Parameter Cards

<u>Columns</u>	<u>Contents</u>
3 - 4	53

<u>Columns</u>	<u>Contents</u>
7 - 8 11 - 12 }	Section number for section <u>n</u> , Section number for section <u>m</u> , where the sections <u>n</u> and <u>m</u> are connected either as adjacent (but $m \neq n+1$) sections of shaft or by a spring. If a section, <u>n</u> , is connected by spring to ground, then <u>m</u> <u>must be</u> 0. When numbering the shaft sections for whirling calculations one must insure that $ n-m \leq 6$ at <u>present</u> .
15 - 16	System number.
17 - 24	$(k_{n,m})_y$ Spring constant in y direction for the connection.
25 - 32 (Specified for spring connections)	$(c_{n,m})_y$ Constant damping coefficient in y direction for the connection.
33 - 40	$(c_{n,m}/\Omega)_y$ Coefficient for frequency dependent damping in y direction for the connection.
41 - 48	$(\Delta x)_{n,m}$
49 - 56 (Specified for rigid connections)	$(\Delta x/KAG)_{n,m}$
57 - 64 only.)	$(\tau_d \Delta x)_{n,m}$
65 - 72	$(Q_{n,m})_y$

12) Special Connection Parameter Cards (Continuation)

<u>Columns</u>	<u>Contents</u>
1 - 16	Blank
17 - 24	$(\tau \Delta x)_{n,m}$
25 - 32	$(k_\alpha \Delta x)_{n,m}$
33 - 40	$(k_\beta \Delta x)_{n,m}$

<u>Columns</u>	<u>Contents</u>
41 - 48	$(k_{n,m})_z$
49 - 56	$(c_{n,m})_z$
57 - 64	$(c_{n,m}/\Omega)_z$
65 - 72	$(Q_{n,m})_z$

13) Scaling Factor Cards for Parameters in Special Connections

<u>Columns</u>	<u>Contents</u>
3 - 4	<u>51</u> if this card contains real parts of scaling factors.
	<u>52</u> if this card contains the imaginary parts of scaling factors.
15 - 16	System number for which scaling factors on this card are to be applied.
17 - 72	Scaling factor for each parameter is given in those columns containing that parameter value on the special connection parameter cards.

14) Scaling Factor Cards for Parameters in Special Connections
(Continuation)

<u>Columns</u>	<u>Contents</u>
1 - 16	Blank
17 - 72	Scaling factor for each parameter given in those columns containing that parameter value on the continuation cards associated with the special connection parameter cards.

15) Microfilm Recorder Plotting Characters

<u>Columns</u>	<u>Contents</u>
3 - 4	60
7 - 12	Blank
13 - 18	$\Delta\Delta\Delta\Delta+$

<u>Columns</u>	<u>Contents</u>
19 - 24	ΔΔΔΔΔ0
25 - 30	ΔΔΔΔΔx
31 - 36	ΔΔΔΔΔ-
37 - 42	ΔΔΔΔΔ.

16) Natural Frequency Card

<u>Columns</u>	<u>Contents</u>
3 - 4	70
9 - 10	Number of natural frequencies desired.

17) Begin a complete new set of data

<u>Columns</u>	<u>Contents</u>
3 - 4	98

18) End of data

<u>Columns</u>	<u>Contents</u>
3 - 4	99

IV. Data Input Forms

PROG. NO.	PROGRAMMER	DATE
PROBLEM NO.	PHASE	SHEET OF
	LABEL	
DATA CONTROL CARD		
NO TYPE NO TYPE etc.		
0090	1 3 5 7 9 11 13 15 17 19 21 23 25 27 29 31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71	
CASE TITLE CARD		
00000(62 HAA)		
OPTION CONTROL CARD		
00200000	OP2 OP3 OP4 OPS OPS OPT OPS OP9 OP10	
00210000	3 17 21 15 19 33 37 41 45	
EDIT CONTROL CARD		
0030	3 13 17 21 25 29	
GENERAL DATA CARD		
0031	$\Delta \Omega_1 (\text{CPS})$ $\Delta \Omega_2 (\text{CPS})$ $\Delta \Omega_3 (\text{CPS})$ h	
0031	9 17 25 33	
SYSTEMS DATA CARDS		
0031	RADIUS INITIAL J	
0031		

Figure 1 Data Input Form (1)

PROBLEM NO. _____ DATE _____
 PHASE _____ LABEL SHEET _____ OF _____

SECTION DATA CARDS

5 9 13 17 25 33 41 49 57 65 73

REAL PART OF SCALING FACTORS

SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU \cdot \Delta x)_{n,n+1}$	$(P_n)_z$
0041 0000 0000				$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$			
	BLANK	→							

SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU \cdot \Delta x)_{n,n+1}$	$(P_n)_z$
0041 0000 0000				$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$			
	BLANK	→							

SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU \cdot \Delta x)_{n,n+1}$	$(P_n)_z$
0041 0000 0000				$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$			
	BLANK	→							

SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU \cdot \Delta x)_{n,n+1}$	$(P_n)_z$
0042 0000 0000				$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$			
	BLANK	→							

SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU \cdot \Delta x)_{n,n+1}$	$(P_n)_z$
0042 0000 0000				$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$			
	BLANK	→							

SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU \cdot \Delta x)_{n,n+1}$	$(P_n)_z$
0042 0000 0000				$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$			
	BLANK	→							

Figure 2 Data Input Form (x)

SECTION PARAMETER VALUES - UN-SCALED									
5	9	13	17	21	25	31	41	49	57
SECTION NO.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUD \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$
0043									
BLANK →									
0043	SECTION NO.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUD \cdot \Delta x)_{n,n+1}$
BLANK ←									
0043	SECTION NO.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUD \cdot \Delta x)_{n,n+1}$
BLANK →									
0043	SECTION NO.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUD \cdot \Delta x)_{n,n+1}$
BLANK ←									
0043	SECTION NO.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUD \cdot \Delta x)_{n,n+1}$
BLANK →									
0043	SECTION NO.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUD \cdot \Delta x)_{n,n+1}$
BLANK ←									

Figure 3 Data Input Form (3)

PROBLEM NO. _____

PROGRAMMER
PHASE

DATE _____
SHEET _____

SPECIAL CONNECTION CARDS

Figure 4 Data Input Form (#)

TIME _____
PROBLEM NO. _____

PROGRAMMER _____
PHASE _____

DATE _____
SHEET _____ OF _____

SPECIAL CONNECTIONS PARAMETER VALUES

5	9	13	17	25	33	41	49	57	65
n	m	SYSTEM	(K _{n,m}) _y	(C _{n,m} /a) _y	(ax) _{n,m}	(ay/KAG) _{n,m}	(TRUD·ax) _{n,m}	(Q _{n,m}) _y	
0.053			(TRU·ax) _{n,m}	(KA·ax) _{n,m}	(KB·ax) _{n,m}	(C _{n,m}) _z	(C _{n,m} /a) _z	(C _{n,m}) _z	
		BLANK	→						
0.053		n m SYSTEM	(K _{n,m}) _y	(C _{n,m} /a) _y	(ax) _{n,m}	(ay/KAG) _{n,m}	(TRUD·ax) _{n,m}	(Q _{n,m}) _y	
			(TRU·ax) _{n,m}	(KA·ax) _{n,m}	(KB·ax) _{n,m}	(C _{n,m}) _z	(C _{n,m} /a) _z	(C _{n,m}) _z	
0.053		BLANK	→						
0.053		n m SYSTEM	(K _{n,m}) _y	(C _{n,m} /a) _y	(ax) _{n,m}	(ay/KAG) _{n,m}	(TRUD·ax) _{n,m}	(Q _{n,m}) _y	
			(TRU·ax) _{n,m}	(KA·ax) _{n,m}	(KB·ax) _{n,m}	(C _{n,m}) _z	(C _{n,m} /a) _z	(C _{n,m}) _z	
0.053		BLANK	→						
0.053		n m SYSTEM	(K _{n,m}) _y	(C _{n,m} /a) _y	(ax) _{n,m}	(ay/KAG) _{n,m}	(TRUD·ax) _{n,m}	(Q _{n,m}) _y	
			(TRU·ax) _{n,m}	(KA·ax) _{n,m}	(KB·ax) _{n,m}	(C _{n,m}) _z	(C _{n,m} /a) _z	(C _{n,m}) _z	
0.053		BLANK	→						
0.053		n m SYSTEM	(K _{n,m}) _y	(C _{n,m} /a) _y	(ax) _{n,m}	(ay/KAG) _{n,m}	(TRUD·ax) _{n,m}	(Q _{n,m}) _y	
			(TRU·ax) _{n,m}	(KA·ax) _{n,m}	(KB·ax) _{n,m}	(C _{n,m}) _z	(C _{n,m} /a) _z	(C _{n,m}) _z	
0.053		BLANK	→						
0.053		n m SYSTEM	(K _{n,m}) _y	(C _{n,m} /a) _y	(ax) _{n,m}	(ay/KAG) _{n,m}	(TRUD·ax) _{n,m}	(Q _{n,m}) _y	
			(TRU·ax) _{n,m}	(KA·ax) _{n,m}	(KB·ax) _{n,m}	(C _{n,m}) _z	(C _{n,m} /a) _z	(C _{n,m}) _z	
0.053		BLANK	→						

Figure 5 Data Input Form (5)

TITLE	PROGRAMMER	DATE
PROBLEM NO.	PHASE	SHEET OF
	LABEL <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	
CHARACTER PLOTTING CHARACTERS		
<u>3</u> <u>4</u>	<u>7</u> <u>13</u>	<u>19</u> <u>25</u>
<u>00</u> <u>60</u>	<u>00</u> <u>BLANK</u>	<u>31</u> <u>37</u> <u>43</u>
NATURAL FREQUENCY SELECTION CARD		
<u>3</u> <u>4</u>	<u>9</u> <u>11</u>	
00	70	0000
START NEW DATA SET CARD		
<u>3</u> <u>4</u>		
00	98	
END OF DATA CARD		
<u>3</u> <u>4</u>		
00	99	

Figure 6 Data Input Form (6)

V. Application with Comparison of Calculated Results

Two sample calculations have been made with GBRC3 in order to obtain results for comparing with an earlier AML whirling vibration program.

The data used in these calculations is for the propeller shaft of the USS Observation Island (EAG-154). The first three critical whirling frequencies are calculated for the shaft in air using for the ratio of spin to whirl a value of 1 in Problem number 1 and a value of $\frac{1}{4}$ in Problem 2.

The computed mode shapes of the shaft are presented in both tabular and graphic forms. The comparison of results is shown in Table 1 immediately following the output.

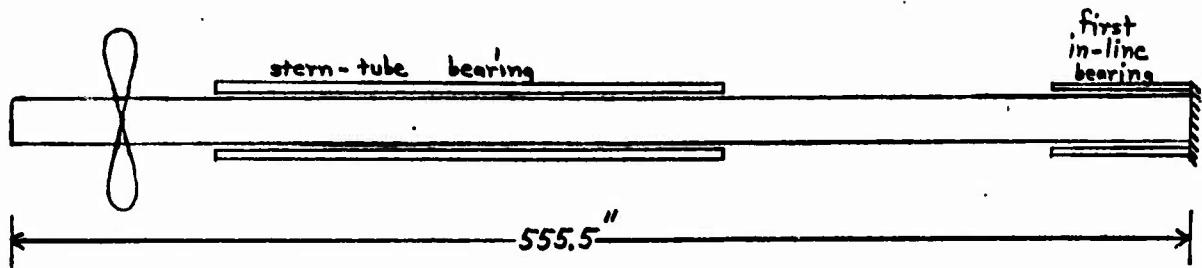


Figure 7
USS Observation Island (EAG-154) Propeller Shaft

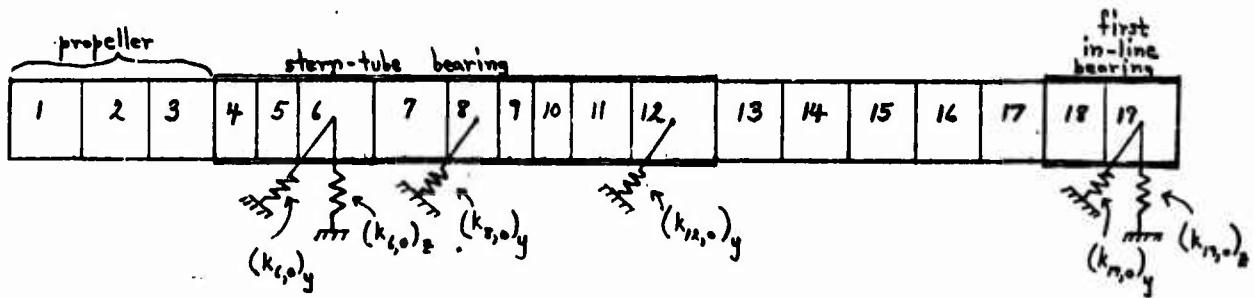
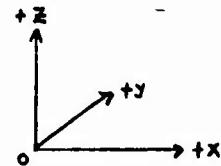


Figure 8
Mathematical Model of the Propeller Shaft
Used for Whirling Calculations

Problem 1. The data is shown as it is prepared on the input forms from which the cards are keypunched.

For these calculations, the large spring constants required to bring about the constraint on deflection at the fixed end of the shaft are read in on a special connection card (type "53"). This card is seen as the last card filled in on the Data Input Form on page . In a later version of GBRC3 this additional data card will not be necessary. The value of such spring constants for fixed ends in the system will automatically be supplied by the program when the end condition designating integer 0002 is given with these sections on the Data Input Forms.

Title: USS OBSERVATION, ISLAND, WHIRLING CALCULATION PROGRAMMER
 PROBLEM NO. 1 DATE _____
 PHASE _____ SHEET 1 OF 1

RUN TITLE CARD
COOCOC(62 HAD SAMPLE PROBLEM 1

DATA CONTROL CARD

NO TYPE NO TYPE etc.

009001	10	01	20	01	30	01	41	19	49	02	51	04	53	01	70	01	60
5	7	9	11	13	17	19	21	23	25	27	29	31	33	35	37	39	41

CASE TITLE CARD

001030(62 HAD USS A OBSERVATION A ISLAND, WHIRLING & FREQUENCIES, - AIR, A H=1

OPTION CONTROL CARD

OP1	OP2	OP3	OP4	OP5	OP6	OP7	OP8	OP9	OP10
00000	00001	00002	00003	00004	00005	00006	00007	00008	00009
5	13	17	21	25	29	33	37	41	45

EDIT CONTROL CARD

0021000	?	13	17	21	25	29

GENERAL DATA CARD
No. 2, (CPS) $\Delta \omega_2$ (CPS) $\Delta \omega_2$ (CPS) h

0030	0019	1.0	30.0	1.0	1.0	35
5	9		25			

SYSTEMS DATA CARDS
SYSTEMS RADIUS INITIAL J

0031			
0031			

TITLE USS DESEURVATION ISLAND, WHIRLING CALCULATION PROGRAMMER _____
 PROBLEM NO. 1 DATE _____

PHASE _____ SHEET 2 OF 9

SECTION DATA CARDS

5 9 13 17

25 33 41

49 57 65

73

REAL PART OF SCALING FACTORS

END CONDN. SYSTEM MASS WATER INERTIA $(\Delta x/EI)_n$ $(\Delta x)_{n,n+1}$ $(\Delta x/KAG)_{n,n+1}$ $(TAU \cdot \Delta x)_{n,n+1}$ $(P_n)_x$

0041 0000 0000 0001 1.0

$(TRU \cdot \Delta x)_{n,n+1}$

$(KA \cdot \Delta x)_{n,n+1}$

$(KB \cdot \Delta x)_{n,n+1}$

$(P_n)_z$

BLANK

END CONDN. SYSTEM MASS WATER INERTIA $(\Delta x/EI)_n$ $(\Delta x)_{n,n+1}$ $(\Delta x/KAG)_{n,n+1}$ $(TAU \cdot \Delta x)_{n,n+1}$ $(P_n)_y$

0041 0000 0000 0000

$(TRU \cdot \Delta x)_{n,n+1}$

$(KA \cdot \Delta x)_{n,n+1}$

$(KB \cdot \Delta x)_{n,n+1}$

$(P_n)_z$

BLANK

END CONDN. SYSTEM MASS WATER INERTIA $(\Delta x/EI)_n$ $(\Delta x)_{n,n+1}$ $(\Delta x/KAG)_{n,n+1}$ $(TAU \cdot \Delta x)_{n,n+1}$ $(P_n)_y$

0041 0000 0000 0000

$(TRU \cdot \Delta x)_{n,n+1}$

$(KA \cdot \Delta x)_{n,n+1}$

$(KB \cdot \Delta x)_{n,n+1}$

$(P_n)_z$

BLANK

IMAGINARY PART OF SCALING FACTORS

END CONDN. SYSTEM MASS WATER INERTIA $(\Delta x/EI)_n$ $(\Delta x)_{n,n+1}$ $(\Delta x/KAG)_{n,n+1}$ $(TAU \cdot \Delta x)_{n,n+1}$ $(P_n)_y$

0042 0000 0000

$(TRU \cdot \Delta x)_{n,n+1}$

$(KA \cdot \Delta x)_{n,n+1}$

$(KB \cdot \Delta x)_{n,n+1}$

$(P_n)_z$

BLANK

END CONDN. SYSTEM MASS WATER INERTIA $(\Delta x/EI)_n$ $(\Delta x)_{n,n+1}$ $(\Delta x/KAG)_{n,n+1}$ $(TAU \cdot \Delta x)_{n,n+1}$ $(P_n)_y$

0042 0000 0000

$(TRU \cdot \Delta x)_{n,n+1}$

$(KA \cdot \Delta x)_{n,n+1}$

$(KB \cdot \Delta x)_{n,n+1}$

$(P_n)_z$

BLANK

TITLE USS OBSERVATION ISLAND, WHIRLING CALCULATION
PROBLEM NO. 1

PROGRAMMER _____ DATE _____
PHASE _____ SHEET 3 OF 9

LABEL

SECTION PARAMETER VALUES - UNSCALED

5	9	13	17	25	35	41	49	57	65	73
SECTION No.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU\cdot\Delta x)_{n,n+1}$	$(P_n)_x$
0043 0001	0001	0001	0001	51.9		15.31	32.0	$\Delta 3.2 E-06$.005788	
<hr/>										
← BLANK →	.001158									
SECTION No.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU\cdot\Delta x)_{n,n+1}$	$(P_n)_y$
0043 0002	0002	0001	0001	51.9		$\Delta 1.0 E-15$	32.0	$\Delta 3.2 E-06$	7.235	
<hr/>										
← BLANK →	1.447									
SECTION No.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU\cdot\Delta x)_{n,n+1}$	$(P_n)_y$
0043 0003	0003	0001	0001	51.9		$\Delta 1.0 E-15$	32.0	$\Delta 1.9 E-06$	7.235	
<hr/>										
← BLANK →	1.447									
SECTION No.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU\cdot\Delta x)_{n,n+1}$	$(P_n)_y$
0043 0004	0004	0001	0001	1.996		1.2295	6.0	2.2108	.005788	
<hr/>										
← BLANK →	.001158									
SECTION No.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRU\cdot\Delta x)_{n,n+1}$	$(P_n)_y$
0043 0005	0005	0001	0001	11.64		$\Delta 1.721$	35.0	12.896	.01471	
<hr/>										
← BLANK →	.002782									

TITLE USS OBSERVATION ISLAND, WHIRLING CALCULATION PROGRAMMER
 PROBLEM NO. 1

DATE _____
 PHASE _____ SHEET 4 OF 2
 LABEL

SECTION PARAMETER VALUES - UNSCALED

S	9	13	17	25	33	41	49	57	65	73
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TAU \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0006	0001	11.64			7.1721	35.0	12.896	.01491		
BLANK										
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TAU \cdot \Delta x)_{n,n+1}$	$(P_n)_Z$	
0043 0007	0001	11.64			7.1721	35.0	12.896	.01491		
BLANK										
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TAU \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0008	0001	4.99			3.0738	15.0	5.5269	.02233		
BLANK										
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TAU \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0009	0001	4.99			3.0738	15.0	5.5269	.02233		
BLANK										
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TAU \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0010	0001	4.99			3.0738	15.0	5.5269	.02233		
BLANK										

TITLE USS OBSERVATION ISLAND, WHIRLING CALCULATION
 PROBLEM NO. 1

DATE _____
 PHASE _____ SHEET 5 OF 9

SECTION PARAMETER VALUES - UNSCALED

5	9	13	17	25	35	41	49	57	65	73
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta X/EI)_n$	$(\Delta X)_{n,n+1}$	$(\Delta X/KAG)_{n,nH}$	$(TAUD \cdot \Delta X)_{n,nH}$	$(P_n)_Y$	
0043 0011	0001	15.0		9.2213	45.0	16.580				
BLANK			$(TRU \cdot \Delta X)_{n,nH}$	$(KA \cdot \Delta X)_{n,nH}$	$(KB \cdot \Delta X)_{n,nH}$	$(P_n)_Z$				
BLANK			.05842							
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta X/EI)_n$	$(\Delta X)_{n,n+1}$	$(\Delta X/KAG)_{n,nH}$	$(TAUD \cdot \Delta X)_{n,nH}$	$(P_n)_Y$	
0043 0012	0001	10.3		6.3525	31.0	11.422				
BLANK			$(TRU \cdot \Delta X)_{n,nH}$	$(KA \cdot \Delta X)_{n,nH}$	$(KB \cdot \Delta X)_{n,nH}$	$(P_n)_Z$				
BLANK			.02186							
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta X/EI)_n$	$(\Delta X)_{n,n+1}$	$(\Delta X/KAG)_{n,nH}$	$(TAUD \cdot \Delta X)_{n,nH}$	$(P_n)_Y$	
0043 0013	0001	10.3		6.3526	31.0	11.422				
BLANK			$(TRU \cdot \Delta X)_{n,nH}$	$(KA \cdot \Delta X)_{n,nH}$	$(KB \cdot \Delta X)_{n,nH}$	$(P_n)_Z$				
BLANK			.02186							
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta X/EI)_n$	$(\Delta X)_{n,n+1}$	$(\Delta X/KAG)_{n,nH}$	$(TAUD \cdot \Delta X)_{n,nH}$	$(P_n)_Y$	
0043 0014	0001	10.3		6.3525	31.0	11.422				
BLANK			$(TRU \cdot \Delta X)_{n,nH}$	$(KA \cdot \Delta X)_{n,nH}$	$(KB \cdot \Delta X)_{n,nH}$	$(P_n)_Z$				
BLANK			.02186							
SECTION No.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta X/EI)_n$	$(\Delta X)_{n,n+1}$	$(\Delta X/KAG)_{n,nH}$	$(TAUD \cdot \Delta X)_{n,nH}$	$(P_n)_Y$	
0043 0015	0001	10.3		6.3525	31.0	11.422				
BLANK			$(TRU \cdot \Delta X)_{n,nH}$	$(KA \cdot \Delta X)_{n,nH}$	$(KB \cdot \Delta X)_{n,nH}$	$(P_n)_Z$				
BLANK			.02186							

TITLE USS OBSERVATION ISLAND, WHIRLING CALCULATION
 PROBLEM NO. 1

PROGRAMMER _____ DATE _____
 PHASE _____ SHEET 6 OF 9
 LABEL

SECTION PARAMETER VALUES - UNSCALED

	5	9	13	17	25	33	41	49	57	65	73
SECTION NO.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUO \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0016			0001	10.3		6.3525	31.0		11.422	.1093	
					$(TAU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$	$(P_n)_Z$			
← BLANK →	02186										
SECTION NO.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUO \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0017			0001	10.3		6.3525	31.0		11.422	.1093	
					$(TAU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$	$(P_n)_Z$			
← BLANK →	02186										
SECTION NO.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUO \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0018			0001	10.3		6.3525	31.0		11.422	.1093	
					$(TAU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$	$(P_n)_Z$			
← BLANK →	02186										
SECTION NO.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUO \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043 0019 0002 0001			15.0			7.2213					
					$(TAU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$	$(P_n)_Z$			
← BLANK →											
SECTION NO.	END CONDN.	END CONDN.	SYSTEM	MASS	WATER INERTIA	$(\Delta x/EI)_n$	$(\Delta x)_{n,n+1}$	$(\Delta x/KAG)_{n,n+1}$	$(TRUO \cdot \Delta x)_{n,n+1}$	$(P_n)_Y$	
0043											
					$(TRU \cdot \Delta x)_{n,n+1}$	$(KA \cdot \Delta x)_{n,n+1}$	$(KB \cdot \Delta x)_{n,n+1}$	$(P_n)_Z$			
← BLANK →											

TITLE USS OBSERVATION ISLAND, WHIRLING CALCULATION
 PROBLEM NO. 1

PROGRAMMER _____ DATE _____
 PHASE _____ SHEET 2 OF 2
 LABEL

SPECIAL CONNECTION CARDS

5 9 13 17 25 33 41 49 57 65 73

REAL PART OF SCALING FACTORS

0051	n m	SYSTEM	$(K_{n,m})_r$	$(C_{n,m})_r$	$(C_{n,m}/\alpha)_r$	$(\Delta x)_{n,m}$	$(\Delta x/KAG)_{n,m}$	$(TAUD \cdot \Delta x)_{n,m}$	$(Q_{n,m})_r$
0051	0001	0001.0 E 6							
BLANK			$(TAU \cdot \Delta x)_{n,m}$	$(KA \cdot \Delta x)_{n,m}$	$(KB \cdot \Delta x)_{n,m}$	$(K_{n,m})_z$	$(C_{n,m})_z$	$(C_{n,m}/\alpha)_z$	$(Q_{n,m})_z$
0051	n m	SYSTEM	$(K_{n,m})_r$	$(C_{n,m})_r$	$(C_{n,m}/\alpha)_r$	$(\Delta x)_{n,m}$	$(\Delta x/KAG)_{n,m}$	$(TAUD \cdot \Delta x)_{n,m}$	$(Q_{n,m})_r$
0051	0002	0002.0 E 16							
BLANK			$(TAU \cdot \Delta x)_{n,m}$	$(KA \cdot \Delta x)_{n,m}$	$(KB \cdot \Delta x)_{n,m}$	$(K_{n,m})_z$	$(C_{n,m})_z$	$(C_{n,m}/\alpha)_z$	$(Q_{n,m})_z$
0051	n m	SYSTEM	$(K_{n,m})_r$	$(C_{n,m})_r$	$(C_{n,m}/\alpha)_r$	$(\Delta x)_{n,m}$	$(\Delta x/KAG)_{n,m}$	$(TAUD \cdot \Delta x)_{n,m}$	$(Q_{n,m})_r$
BLANK			$(TAU \cdot \Delta x)_{n,m}$	$(KA \cdot \Delta x)_{n,m}$	$(KB \cdot \Delta x)_{n,m}$	$(K_{n,m})_z$	$(C_{n,m})_z$	$(C_{n,m}/\alpha)_z$	$(Q_{n,m})_z$

IMAGINARY PART OF SCALING FACTORS

0052	n m	SYSTEM	$(K_{n,m})_r$	$(C_{n,m})_r$	$(C_{n,m}/\alpha)_r$	$(\Delta x)_{n,m}$	$(\Delta x/KAG)_{n,m}$	$(TAUD \cdot \Delta x)_{n,m}$	$(Q_{n,m})_r$
BLANK			$(TAU \cdot \Delta x)_{n,m}$	$(KA \cdot \Delta x)_{n,m}$	$(KB \cdot \Delta x)_{n,m}$	$(K_{n,m})_z$	$(C_{n,m})_z$	$(C_{n,m}/\alpha)_z$	$(Q_{n,m})_z$
0052	n m	SYSTEM	$(K_{n,m})_r$	$(C_{n,m})_r$	$(C_{n,m}/\alpha)_r$	$(\Delta x)_{n,m}$	$(\Delta x/KAG)_{n,m}$	$(TAUD \cdot \Delta x)_{n,m}$	$(Q_{n,m})_r$
BLANK			$(TAU \cdot \Delta x)_{n,m}$	$(KA \cdot \Delta x)_{n,m}$	$(KB \cdot \Delta x)_{n,m}$	$(K_{n,m})_z$	$(C_{n,m})_z$	$(C_{n,m}/\alpha)_z$	$(Q_{n,m})_z$

Data Input Form: (#)

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TITLE USS OBSERVATION ISLAND, WHIRLING CALCULATION PROGRAMMER
PROBLEM NO. 1

DATE _____
PHASE _____
LABEL SHEET 8 OF 2

SPECIAL CONNECTIONS PARAMETER VALUES

	5	9	13	17	25	33	41	49	57	65	73
	n	m	SYSTEM	(Kn,m) _y	(Cn,m) _y	(Cn,m/n) _y	(ax) _{n,m}	(ΔY/KAG) _{n,m}	(TRUD·ΔX) _{n,m}	(Qn,m) _y	
0.053	0006	0000	0001	9.703							
	BLANK	→		(TRU·ΔX) _{n,m}	(KA·ΔX) _{n,m}	(KB·ΔX) _{n,m}	(Kn,m)	(Cn,m)	(Cn,m/n)	(Qn,m)	
	n	m	SYSTEM	(Kn,m) _y	(Cn,m) _y	(Cn,m/n) _y	(ax) _{n,m}	(ΔY/KAG) _{n,m}	(TRUD·ΔX) _{n,m}	(Qn,m) _y	
0.053	0008	0000	0001	4.366							
	BLANK	→		(TRU·ΔX) _{n,m}	(KA·ΔX) _{n,m}	(KB·ΔX) _{n,m}	(Kn,m)	(Cn,m)	(Cn,m/n)	(Qn,m)	
	n	m	SYSTEM	(Kn,m) _y	(Cn,m) _y	(Cn,m/n) _y	(ax) _{n,m}	(ΔY/KAG) _{n,m}	(TRUD·ΔX) _{n,m}	(Qn,m) _y	
0.053	0012	0000	0001	1.31							
	BLANK	→		(TRU·ΔX) _{n,m}	(KA·ΔX) _{n,m}	(KB·ΔX) _{n,m}	(Kn,m)	(Cn,m)	(Cn,m/n)	(Qn,m)	
	n	m	SYSTEM	(Kn,m) _y	(Cn,m) _y	(Cn,m/n) _y	(ax) _{n,m}	(ΔY/KAG) _{n,m}	(TRUD·ΔX) _{n,m}	(Qn,m) _y	
0.053	0019	0000	0002	1.0							
	BLANK	→		(TRU·ΔX) _{n,m}	(KA·ΔX) _{n,m}	(KB·ΔX) _{n,m}	(Kn,m)	(Cn,m)	(Cn,m/n)	(Qn,m)	
	n	m	SYSTEM	(Kn,m) _y	(Cn,m) _y	(Cn,m/n) _y	(ax) _{n,m}	(ΔY/KAG) _{n,m}	(TRUD·ΔX) _{n,m}	(Qn,m) _y	
0.053											
	BLANK	→		(TRU·ΔX) _{n,m}	(KA·ΔX) _{n,m}	(KB·ΔX) _{n,m}	(Kn,m)	(Cn,m)	(Cn,m/n)	(Qn,m)	
	n	m	SYSTEM	(Kn,m) _y	(Cn,m) _y	(Cn,m/n) _y	(ax) _{n,m}	(ΔY/KAG) _{n,m}	(TRUD·ΔX) _{n,m}	(Qn,m) _y	
0.053											
	BLANK	→									

TITLE	PROGRAMMER	DATE						
PROBLEM NO.	PHASE	SHEET <u>9</u> OF <u>9</u>						
CHARACTRON PLOTTING CHARACTERS								
3 4	7	13	19	25	31	37	43	
00	60	00	BLANK	△△△△△	0	△△△△△ X	△△△△△ -	△△△△△ •
NATURAL FREQUENCY SELECTION CARD								
3 4	9	"						
00	70	000003						
START NEW DATA SET CARD								
3 4	98	"						
00	99	"						
END OF DATA CARD								
3 4	99	"						
00	99	"						

Data Inbut Form (a)

GBRC3 OCT 7, 1966
SAMPLE PROBLEM 1

DATA CONTROL CARD

NC TYPE

1 10

1 20

1 30

1 41

1 43

2 51

4 53

1 70

1 60

CASE TITLE-USS OBSERVATION ISLAND. WHIRLING FREQUENCIES.-AIR. H=1

OPTION DATA

20 -0 2 -0 1 -0 1 -0 -0 -0 1

GENERAL DATA - NUMBER OF SECTIONS 19
WHIRLING FREQUENCY RANGE FROM
FREQUENCY INTERVAL 1.000 CPS
RATIO OF SPIN TO WHIRL = 1.0000

1.000 CPS TD 30.000 CPS

DX/EI(N) 1.0000E-11

DX/KAG(N,N+1) 1.0000E-09

TAUDDX(N,N+1) 1.0000E-04

P(N)/V 1.0000E-00

REAL PARTS OF SCALING FACTORS

SECTION-END CONDON-SYSTEM MASS WATER INERTIA

1 1.0000E 00 -0.

DX/EI(N) 1.0000E-11

DX/KAG(N,N+1) 1.0000E-09

TAUDDX(N,N+1) 1.0000E-04

P(N)/V 1.0000E-00

PARAMETER VALUES FOR EACH SECTION - UNSCALED

SECTION-END CONDON-SYSTEM MASS WATER INERTIA

1 5.1900E 01 -0.

DX/EI(N) 1.5310E-01

DX/KAG(N,N+1) 3.2000E-06

TAUDDX(N,N+1) 5.7880E-03

P(N)/V -0.

TAUDDX(N,N+1) KA*DDX(N,N+1)

1.1580E-03 -0.

KB*DDX(N,N+1) -0.

P(N)/Z -0.

2 0 1 MASS WATER INERTIA

5.1900E 01 -0.

DX/EI(N) 1.0000E-15

DX/KAG(N,N+1) 3.2000E-06

TAUDDX(N,N+1) 7.2350E-06

P(N)/V -0.

TAUDDX(N,N+1) KA*DDX(N,N+1)

1.4470E 00 -0.

KB*DDX(N,N+1) -0.

P(N)/Z -0.

3 0 1 MASS WATER INERTIA

5.1900E 01 -0.

DX/EI(N) 1.0000E-15

DX/KAG(N,N+1) 3.2000E-06

TAUDDX(N,N+1) 7.2350E-06

P(N)/V -0.

4 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{1.2295E-00}$ $\frac{DX/KAG(N,N+1)}{6.0000E-00}$ $\frac{TAUD*DX(N,N+1)}{2.2108E-00}$ $\frac{P(N)/Y}{5.7880E-03}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $1.1580E-03$ -0.
 $-0.$

5 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{7.1721E-00}$ $\frac{DX/KAG(N,N+1)}{3.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{1.2896E-01}$ $\frac{P(N)/Y}{1.4910E-02}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $2.9820E-03$ -0.
 $-0.$

6 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{7.1721E-00}$ $\frac{DX/KAG(N,N+1)}{3.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{1.2896E-01}$ $\frac{P(N)/Y}{1.4910E-02}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $2.9820E-03$ -0.
 $-0.$

7 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{7.1721E-00}$ $\frac{DX/KAG(N,N+1)}{3.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{1.2896E-01}$ $\frac{P(N)/Y}{1.4910E-02}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $2.9820E-03$ -0.
 $-0.$

8 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{3.0738E-00}$ $\frac{DX/KAG(N,N+1)}{1.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{5.5269E-01}$ $\frac{P(N)/Y}{2.2330E-02}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $4.4660E-03$ -0.
 $-0.$

9 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{3.0738E-00}$ $\frac{DX/KAG(N,N+1)}{1.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{5.5269E-01}$ $\frac{P(N)/Y}{2.2330E-02}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $4.4660E-03$ -0.
 $-0.$

10 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{3.0738E-00}$ $\frac{DX/KAG(N,N+1)}{1.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{5.5269E-01}$ $\frac{P(N)/Y}{2.2330E-02}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $4.4660E-03$ -0.
 $-0.$

11 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{9.2213E-00}$ $\frac{DX/KAG(N,N+1)}{4.5000E-01}$ $\frac{TAUD*DX(N,N+1)}{1.6580E-01}$ $\frac{P(N)/Y}{2.9210E-01}$ -0.
 $TAU*DX(N,N+1) KA*DX(N,N+1)$ $KB*DX(N,N+1)$ $P(N)/Z$
 $5.8420E-02$ -0.
 $-0.$

12 0 1 MASS WATER INERTIA $\frac{DX/EI(N)}{6.3525E-00}$ $\frac{DX/KAG(N,N+1)}{3.1000E-01}$ $\frac{TAUD*DX(N,N+1)}{1.1422E-01}$ $\frac{P(N)/Y}{1.0930E-01}$ -0.

			$\text{TAU}^{\star}\text{DX}(N, I+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KB}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
13	0	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KR}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
14	0	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KB}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
15	0	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KB}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
16	0	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KB}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
17	0	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KB}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
18	0	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KR}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$2.1860E-02$	$-0.$	$-0.$
			MASS	WATER INERTIA	$\text{DX}/\text{EI}(N)$
			$1.0330E 01$	$-0.$	$6.3525E 00$
19	2	1	$\text{TAU}^{\star}\text{DX}(N, N+1) \text{KA}^{\star}\text{DX}(N, N+1)$	$\text{KR}^{\star}\text{DX}(N, N+1)$	$P(N)/Z$
			$-0.$	$-0.$	$-0.$

REAL PARTS OF SCALING FACTORS

N	M	SYSTEM	$K(N, M)/Y$	$C(N, M)/Y$	$DX/KAG(N, M)$	$TAU^{\star}\text{DX}(N, M)$	$Q(N, M)/Y$
	1	$1.0000E 06$	$-0.$	$-0.$	$-0.$	$-0.$	$-0.$
		$\text{TAU}^{\star}\text{DX}(N, M)$	$\text{KA}^{\star}\text{DX}(N, M)$	$\text{KB}^{\star}\text{DX}(N, M)$	$K(N, M)/Z$	$C(N, M)/Z$	$Q(N, M)/Z$

	-0.	-0.	-0.	1.0000E 09	-0.	-0.	-0.	
?	K(N,M)/Y 1.0000E 16	C(N,M)/Y -0.	C(N,M)/W/Y -0.	DX(N,M) -0.	Dx/KAG(N,M) -0.	TAUD*DX(N,M) -0.	Q(N,M)/Y -0.	
	TAU*DX(N,M)	KA*DX(N,M)	KH*DX(N,M)	K(N,M)/Z 1.0000E 16	C(N,M)/Z -0.	C(N,M)/W/Z -0.	Q(N,M)/Z -0.	
PARAMETER VALUES FOR SPECIAL CONNECTIONS								
N	M	SYSTEM	K(N,M)/Y	C(N,M)/Y	DX(N,M)	TAUD*DX(N,M)	Q(N,M)/Y	
6	0	1	9.7030E 00	-0.	-0.	-0.	-0.	
	TAU*DX(N,M)	KA*DX(N,M)	KD*DX(N,M)	K(N,M)/Z 2.5680E 00	C(N,M)/Z -0.	C(N,M)/W/Z -0.	Q(N,M)/Z -0.	
E	0	1	K(N,M)/Y 4.3660E 00	C(N,M)/Y -0.	DX(N,M) -0.	DX/KAG(N,M) -0.	TAUD*DX(N,M) -0.	
	TAU*DX(N,M)	KA*DX(N,M)	KR*DX(N,M)	K(N,M)/Z -0.	C(N,M)/Z -0.	C(N,M)/W/Z -0.	Q(N,M)/Z -0.	
60	12	0	1	K(N,M)/Y 1.3100E 00	C(N,M)/Y -0.	DX(N,M) -0.	DX/KAG(N,M) -0.	TAUD*DX(N,M) -0.
	TAU*DX(N,M)	KA*DX(N,M)	KR*DX(N,M)	K(N,M)/Z -0.	C(N,M)/Z -0.	C(N,M)/W/Z -0.	Q(N,M)/Z -0.	
I	0	2	K(N,M)/Y 1.0000E 00	C(N,M)/Y -0.	DX(N,M) -0.	DX/KAG(N,M) -0.	TAUD*DX(N,M) -0.	
	TAU*DX(N,M)	KA*DX(N,M)	KH*DX(N,M)	K(N,M)/Z -0.	C(N,M)/Z -0.	C(N,M)/W/Z -0.	Q(N,M)/Z -0.	

NF.RE.Q= 3
 CHAR(1)=
 CHAR(2)=
 CHAR(3)=
 CHAR(4)=
 CHAR(5)=
 CHAR(6)=

SHECS

SAMPLE PROFILE 1

USS OBSERVATION ISLAND. WHIRLING FREQUENCIES.-AIR. H=1

FREQUENCY 6.37 CPS

XY-PLANE

SECTION	DEFLECTIONS				MOMENTS			
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE
1	1.0000E+00	0.0000E+00	1.0000E+00	0.0000E+00	7.4734E-06	-0.0000E+00	7.4734E-06	-0.0000E+00
2	7.0385E-01	-0.0000E+00	7.6085E-01	-3.0000E+00	-2.6623E+00	0.0000E+00	2.6623E+00	0.0000E+00
3	5.2170E-01	-0.0000E+00	5.2170E-01	-0.0000E+00	-1.4111E+07	-0.0000E+00	1.4111E+07	0.0000E+00
4	2.8256E-01	0.0000E+00	2.8256E-01	0.0000E+00	-2.6948E+07	0.0000E+00	2.6948E+07	0.0000E+00
5	2.3928E-01	0.0000E+00	2.3928E-01	0.0000E+00	-2.8097E+07	0.0000E+00	2.8097E+07	0.0000E+00
6	5.7307E-02	0.0000E+00	5.7307E-02	0.0000E+00	-3.4937E+07	0.0000E+00	3.4937E+07	0.0000E+00
7	-2.9807E-02	0.0000E+00	2.9807E-02	0.0000E+00	-2.2349E+07	0.0000E+00	2.2349E+07	0.0000E+00
8	-6.0814E-02	0.0000E+00	6.0814E-02	0.0000E+00	-9.7383E+06	0.0000E+00	9.7383E+06	0.0000E+00
9	-7.1077E-02	0.0000E+00	7.1077E-02	0.0000E+00	-8.3130E+06	0.0000E+00	8.3130E+06	0.0000E+00
10	-7.7505E-02	0.0000E+00	7.7505E-02	0.0000E+00	-6.8778E+06	0.0000E+00	6.8778E+06	0.0000E+00
11	-8.0757E-02	0.0000E+00	8.0757E-02	0.0000E+00	-5.4320E+06	0.0000E+00	5.4320E+06	0.0000E+00
12	-6.7943E-02	0.0000E+00	6.7943E-02	0.0000E+00	-9.9223E+05	0.0000E+00	9.9223E+05	0.0000E+00
13	-5.8165E-02	0.0000E+00	5.8165E-02	0.0000E+00	-6.5124E+05	0.0000E+00	6.5124E+05	0.0000E+00
14	-4.7093E-02	0.0000E+00	4.7093E-02	0.0000E+00	-2.7409E+05	0.0000E+00	2.7409E+05	0.0000E+00
15	-3.5473E-02	0.0000E+00	3.5473E-02	0.0000E+00	1.3124E+05	0.0000E+00	1.3124E+05	0.0000E+00
16	-2.4105E-02	0.0000E+00	2.4105E-02	0.0000E+00	5.5637E+05	0.0000E+00	5.5637E+05	0.0000E+00
17	-1.3827E-02	0.0000E+00	1.3827E-02	0.0000E+00	9.9298E+05	0.0000E+00	9.9298E+05	0.0000E+00
18	-5.5029E-03	0.0000E+00	5.5029E-03	0.0000E+00	1.4332E+06	0.0000E+00	1.4332E+06	0.0000E+00
19	-1.3649E-12	0.0000E+00	1.3649E-12	0.0000E+00	1.8703E+06	0.0000E+00	1.8703E+06	0.0000E+00

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XZ-PLANE

SECTION	DEFLECTIONS				MOMENTS			
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE
1	-0.	3.3229E+00	3.3229E+00	9.0000E+01	-0.	2.5434E-05	2.5434E-05	9.0000E+01
2	-0.	2.5090E+00	2.5090E+00	9.0000E+01	0.	-8.3498E+06	8.3498E+06	-9.0000E+01
3	-0.	1.6951E+00	1.6951E+00	9.0000E+01	0.	-2.9058E+07	2.9058E+07	-9.0000E+01
4	-0.	6.8122E+01	6.8122E+01	9.0000E+01	0.	-5.1779E+07	5.1779E+07	-9.0000E+01
5	-0.	7.3119E+01	7.3119E+01	9.0000E+01	0.	-5.7557E+07	5.7557E+07	-9.0000E+01
6	0.	3.4221E+04	3.4221E+04	9.0000E+01	0.	-8.0057E+07	8.0057E+07	-9.0000E+01
7	0.	5.1821E+01	5.1821E+01	9.0000E+01	0.	-7.1797E+07	7.1797E+07	-9.0000E+01
8	0.	8.5640E+01	8.5640E+01	9.0000E+01	0.	-6.3197E+07	6.3197E+07	-9.0000E+01
9	0.	-9.7217E+01	9.7217E+01	9.0000E+01	0.	-5.7411E+07	5.7411E+07	-9.0000E+01
10	0.	-1.0605E+00	1.0605E+00	9.0000E+01	0.	-5.5507E+07	5.5507E+07	-9.0000E+01
11	0.	-1.1232E+00	1.1232E+00	9.0000E+01	0.	-5.1475E+07	5.1475E+07	-9.0000E+01
12	0.	-1.0972E+00	1.0972E+00	9.0000E+01	0.	-3.8154E+07	3.8154E+07	-9.0000E+01
13	0.	-1.1040E+00	1.1040E+00	9.0000E+01	0.	-2.0413E+07	2.0413E+07	-9.0000E+01
14	0.	-8.5460E+01	8.5460E+01	9.0000E+01	0.	-1.9154E+07	1.9154E+07	-9.0000E+01
15	0.	-6.6931E+01	6.6931E+01	9.0000E+01	0.	-7.4566E+06	7.4566E+06	-9.0000E+01
16	0.	-6.6221E+01	6.6221E+01	9.0000E+01	0.	-3.5846E+06	3.5846E+06	-9.0000E+01
17	0.	-2.7607E+01	2.7607E+01	9.0000E+01	0.	1.4865E+07	1.4865E+07	9.0000E+01
18	0.	-1.1217E+01	1.1217E+01	9.0000E+01	0.	2.6286E+07	2.6286E+07	9.0000E+01
19	0.	-3.6793E+11	-3.6793E+11	-9.0000E+01	0.	3.7760E+07	3.7760E+07	9.0000E+01

GENC3

SAMPLE PROBLEM 1

USS OBSERVATION ISLAND. WHIRLING FREQUENCIES.-AIR. H=1
 FREQUENCY 0.08 CPS

XY-PLANE

SECTION	DEFLECTIONS				MOMENTS		
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART	PHASE ANGLE
1	1.0000E 00	0.	1.0000E 00	0.	7.2791E-06	-0.	7.2791E-06 -0.
2	7.6707E-01	-0.	7.6707E-01	-0.	-4.2835E 06	4.2835E 06	4.2835E 06 -0.
3	5.3414E-01	-0.	5.3414E-01	-0.	-1.2052E 07	1.2052E 07	1.2052E 07 -0.
4	3.0120E-01	0.	3.0120E-01	0.	-2.2108E 07	2.2108E 07	2.2108E 07 -0.
5	2.5870E-01	0.	2.5870E-01	0.	-2.3966E 07	2.3966E 07	2.3966E 07 -0.
6	6.9281E-02	0.	6.9281E-02	0.	-3.5073E 07	3.5073E 07	3.5073E 07 -0.
7	-2.3227E-02	0.	2.3227E-02	0.	-2.2724E 07	2.2724E 07	2.2724E 07 -0.
8	-5.8663E-02	0.	5.8663E-02	0.	-1.0351E 07	1.0351E 07	1.0351E 07 -0.
9	-7.0517E-02	0.	7.0517E-02	0.	-6.6801E 06	6.6801E 06	6.6801E 06 -0.
10	-7.8232E-02	0.	7.8232E-02	0.	-7.3952E 06	7.3952E 06	7.3952E 06 -0.
11	-8.2532E-02	0.	8.2532E-02	0.	-5.8953E 06	5.8953E 06	5.8953E 06 -0.
12	-7.1015E-02	0.	7.1015E-02	0.	-1.0523E 06	1.0523E 06	1.0523E 06 -0.
13	-6.1622E-02	0.	6.1622E-02	0.	-6.8123E 05	6.8123E 05	6.8123E 05 -0.
14	-5.0487E-02	0.	5.0487E-02	0.	-4.6065E 05	4.6065E 05	4.6065E 05 -0.
15	-3.8424E-02	0.	3.8424E-02	0.	-6.6603E 02	6.6603E 02	6.6603E 02 -0.
16	-2.6535E-02	0.	2.6535E-02	0.	-4.9321E 05	4.9321E 05	4.9321E 05 -0.
17	-1.5220E-02	0.	1.5220E-02	0.	-1.0075E 06	1.0075E 06	1.0075E 06 -0.
18	-6.1095E-03	0.	6.1095E-03	0.	-1.5349E 06	1.5349E 06	1.5349E 06 -0.
19	-1.7277E-12	0.	1.7277E-12	0.	-2.0683E 06	2.0683E 06	2.0683E 06 -0.

XZ-PLANE

SECTION	DEFLECTIONS				MOMENTS		
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART	PHASE ANGLE
1	0.	-4.1186E-01	4.1186E-01	3.1244E-01	-9.0000E 01	0.	-3.1069E-06 -9.0000E 01
2	0.	-3.1244E-01	3.1244E-01	0.	-1.7626E 06	1.7626E 06	9.0000E 01
3	0.	-2.1302E-01	2.1302E-01	0.	-2.7283E 06	2.7283E 06	9.0000E 01
4	C	-1.1360E-01	1.1360E-01	0.	-4.6066E 06	4.6066E 06	9.0000E 01
5	0.	-9.5023E-02	9.5023E-02	0.	-5.3614E 06	5.3614E 06	9.0000E 01
6	0.	-5.9375E-05	5.9375E-05	0.	-9.8704E 06	9.8704E 06	9.0000E 01
7	-0.	6.8161E-02	6.8161E-02	0.	-9.0444E 06	9.0444E 06	9.0000E 01
8	-0.	1.1365E-01	1.1365E-01	0.	-8.1479E 06	8.1479E 06	9.0000E 01
9	-0.	1.2938E-01	1.2938E-01	0.	-7.7415E 06	7.7415E 06	9.0000E 01
10	-0.	1.4154E-01	1.4154E-01	0.	-7.3104E 06	7.3104E 06	9.0000E 01
11	-0.	1.5031E-01	1.5031E-01	0.	-6.8520E 06	6.8520E 06	9.0000E 01
12	-0.	1.4809E-01	1.4809E-01	0.	-5.2184E 06	5.2184E 06	9.0000E 01
13	0.	1.3625E-01	1.3625E-01	0.	-3.9696E 06	3.9696E 06	9.0000E 01
14	0.	1.1654E-01	1.1654E-01	0.	-2.6082E 06	2.6082E 06	9.0000E 01
15	0.	9.1685E-02	9.1685E-02	0.	-1.1506E 06	1.1506E 06	9.0000E 01
16	0.	6.4495E-02	6.4495E-02	0.	-3.8282E 05	3.8282E 05	9.0000E 01
17	0.	3.8059E-02	3.8059E-02	0.	-1.9694E 06	1.9694E 06	9.0000E 01
18	0.	1.5490E-02	1.5490E-02	0.	-3.5874E 06	3.5874E 06	9.0000E 01
19	0.	5.2392E-12	5.2392E-12	0.	-5.2180E 06	5.2180E 06	9.0000E 01

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GURC3

SAMPLE PROHLM

USS OBSERVATION ISLAND, WHIRLING FREQUENCIES.-AIR. H=1

FREQUENCY 23.54 CPS

XY-PLANE

SECTION	DEFLECTIONS			MOMENTS			
	REAL PART	IMAG PART	AHS VALUE	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE
1	1.0000E+00	0.	1.0000E+00	0.	2.0567E-06	-0.	2.0567E-06 -0.
2	9.3419E-01	-0.	9.3419E-01	-0.	-3.6702E-07	-0.	1.6702E-07 0.
3	8.6837E-01	-0.	8.6837E-01	-0.	5.0479E-07	0.	5.0479E-07 0.
4	8.0236E-01	0.	8.0236E-01	0.	1.0610E-08	0.	1.0610E-08 0.
5	7.7524E-01	0.	7.7524E-01	0.	8.6797E-07	0.	8.6797E-07 0.
6	3.9547E-01	0.	3.9547E-01	0.	-3.3477E-07	0.	3.3477E-07 0.
7	1.4793E-01	0.	1.4793E-01	0.	-2.3544E-07	0.	2.3544E-07 0.
6	-4.1007E-02	-0.	4.1007E-02	0.	1.5215E-07	0.	1.5215E-07 0.
3	-1.1593E-01	0.	1.1593E-01	0.	-1.5401E-07	0.	1.5401E-07 0.
10	-1.8366E-01	-0.	1.8368E-01	0.	-1.5335E-07	0.	1.5335E-07 0.
11	-2.4425E-01	0.	2.4425E-01	0.	-1.4841E-07	0.	1.4841E-07 0.
12	-3.6304E-01	-0.	3.6304E-01	0.	-1.6658E-07	0.	1.6658E-07 0.
13	-4.1657E-01	0.	4.1657E-01	0.	-2.3786E-07	0.	2.3786E-07 0.
14	-4.2218E-01	-0.	4.2218E-01	0.	-2.4947E-07	0.	2.4947E-07 0.
15	-3.7758E-01	0.	3.7758E-01	0.	-2.0358E-07	-0.	2.0358E-07 0.
16	-2.9191E-01	0.	2.9191E-01	0.	-1.1043E-07	-0.	1.1043E-07 0.
17	-1.8375E-01	0.	1.8375E-01	0.	1.3004E-06	0.	1.3004E-06 0.
18	-7.7670E-02	0.	7.7670E-02	0.	1.4526E-07	0.	1.4526E-07 0.
19	-2.1163E-11	-0.	2.1163E-11	0.	2.6325E-07	0.	2.6325E-07 0.

XZ-PLANE

SECTION	DEFLECTIONS			MOMENTS			
	REAL PART	IMAG PART	AHS VALUE	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE
1	0.	-4.3748E-00	4.3748E-00	-9.0000E-01	0.	-5.0913E-05	-9.0000E-01
2	0.	-2.7456E+00	2.7456E+00	-9.0000E+01	0.	1.5906E-08	9.0000E-01
3	0.	-1.1164E+00	1.1164E+00	-9.0000E+01	0.	4.9194E-08	9.0000E-01
4	0.	5.1285E-01	5.1285E-01	3.0000E+01	0.	8.6539E-08	9.0000E-01
5	0.	7.7513E-01	7.7513E-01	9.0000E+01	0.	9.2142E-08	9.0000E-01
6	0.	-1.0479E-02	1.0479E-02	-9.0000E+01	0.	1.2410E-09	9.0000E-01
7	0.	-4.2583E+00	4.2583E+00	-9.0000E+01	0.	6.1854E-08	9.0000E-01
8	0.	-1.0045E+01	1.0045E+01	-9.0000E+01	0.	3.3902E-07	9.0000E-01
9	0.	-1.2534E+01	1.2534E+01	-9.0000E+01	0.	-2.0080E-08	-9.0000E-01
10	0.	-1.4924E+01	1.4924E+01	-9.0000E+01	0.	-4.1493E-08	-9.0000E-01
11	0.	-1.7113E+01	1.7113E+01	-9.0000E+01	0.	-6.0455E-08	-9.0000E-01
12	0.	-2.1078E+01	2.1078E+01	-9.0000E+01	0.	-9.2426E-08	-9.0000E-01
13	0.	-2.1935E+01	2.1935E+01	-9.0000E+01	0.	-9.9394E-08	-9.0000E-01
14	0.	-2.0779E+01	2.0779E+01	-9.0000E+01	0.	-1.0877E-08	-9.0000E-01
15	0.	-1.77779E+01	1.77779E+01	-9.0000E+01	0.	-6.7695E-08	-9.0000E-01
16	0.	-1.3400E+01	1.3400E+01	-9.0000E+01	0.	-1.3149E-08	-9.0000E-01
17	0.	-6.3577E+00	6.3577E+00	-9.0000E+01	0.	-6.4098E-08	-9.0000E-01
18	0.	-3.5223E+00	3.5223E+00	-9.0000E+01	0.	-1.1743E-09	-9.0000E-01

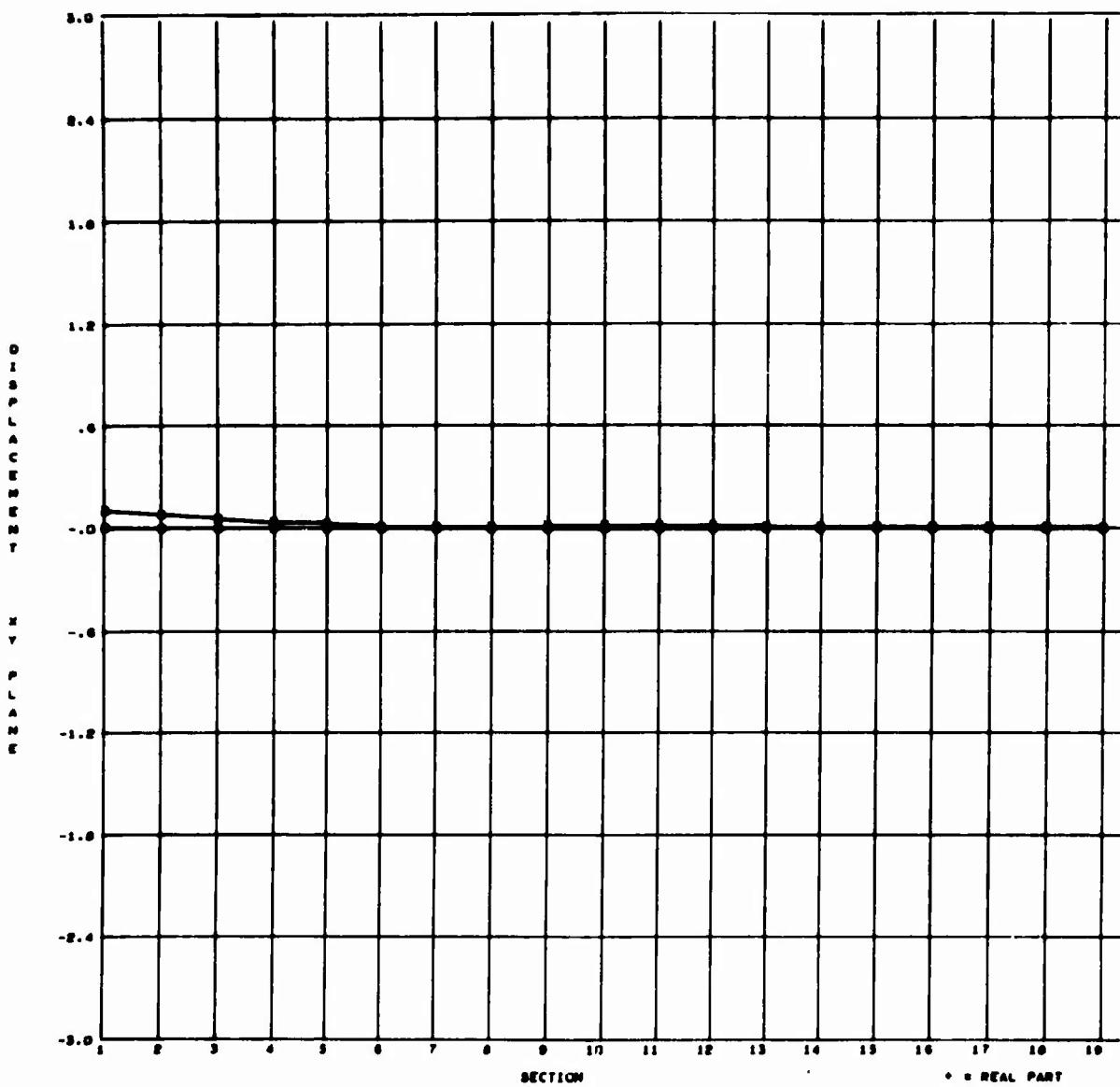
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GBRC3 OCT 7, 1966
SAMPLE PROBLEM 1

DATA CONTROL CARD

NO TYPE

END GBRC3 RUN

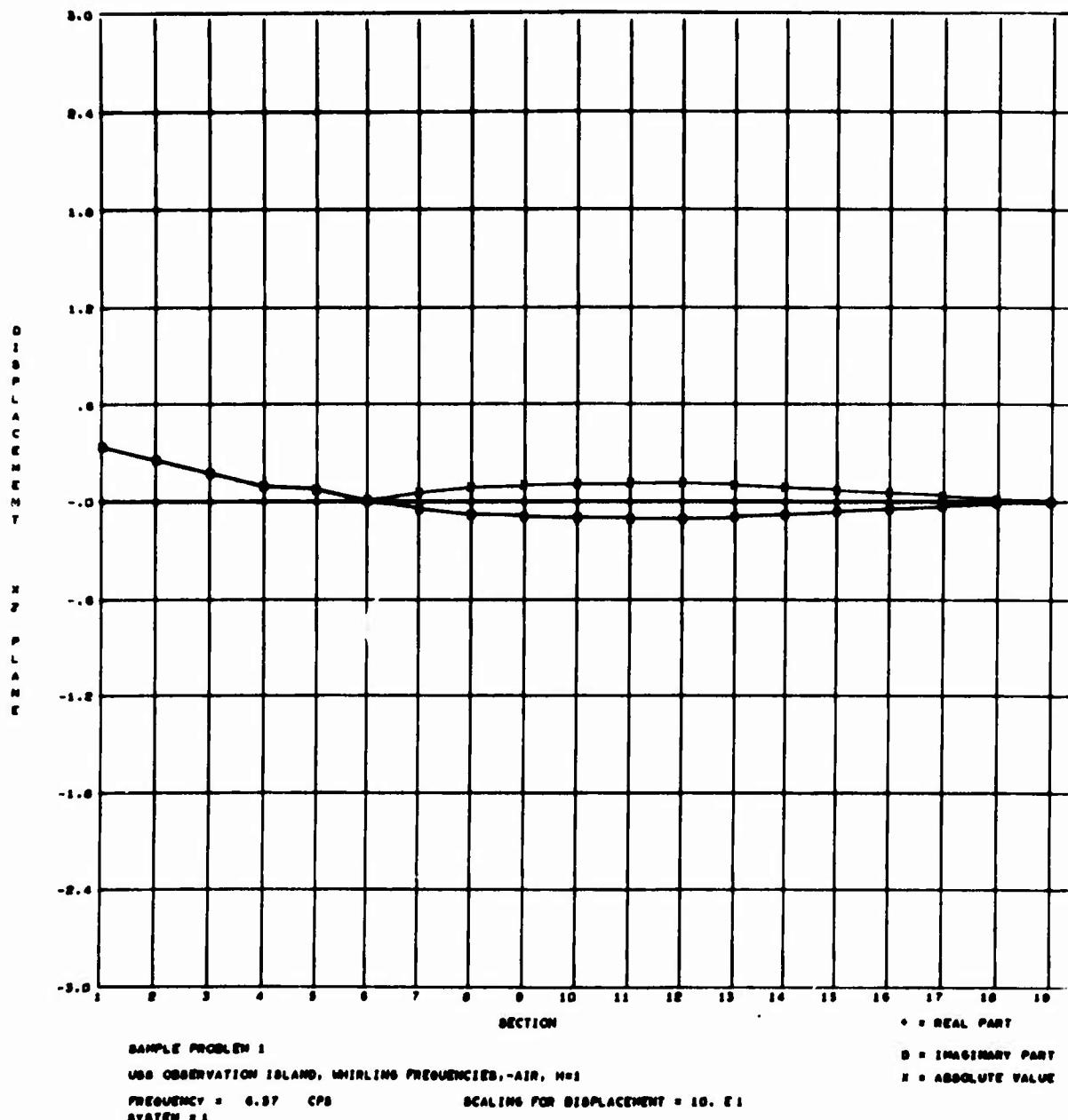


SAMPLE PROBLEM 1

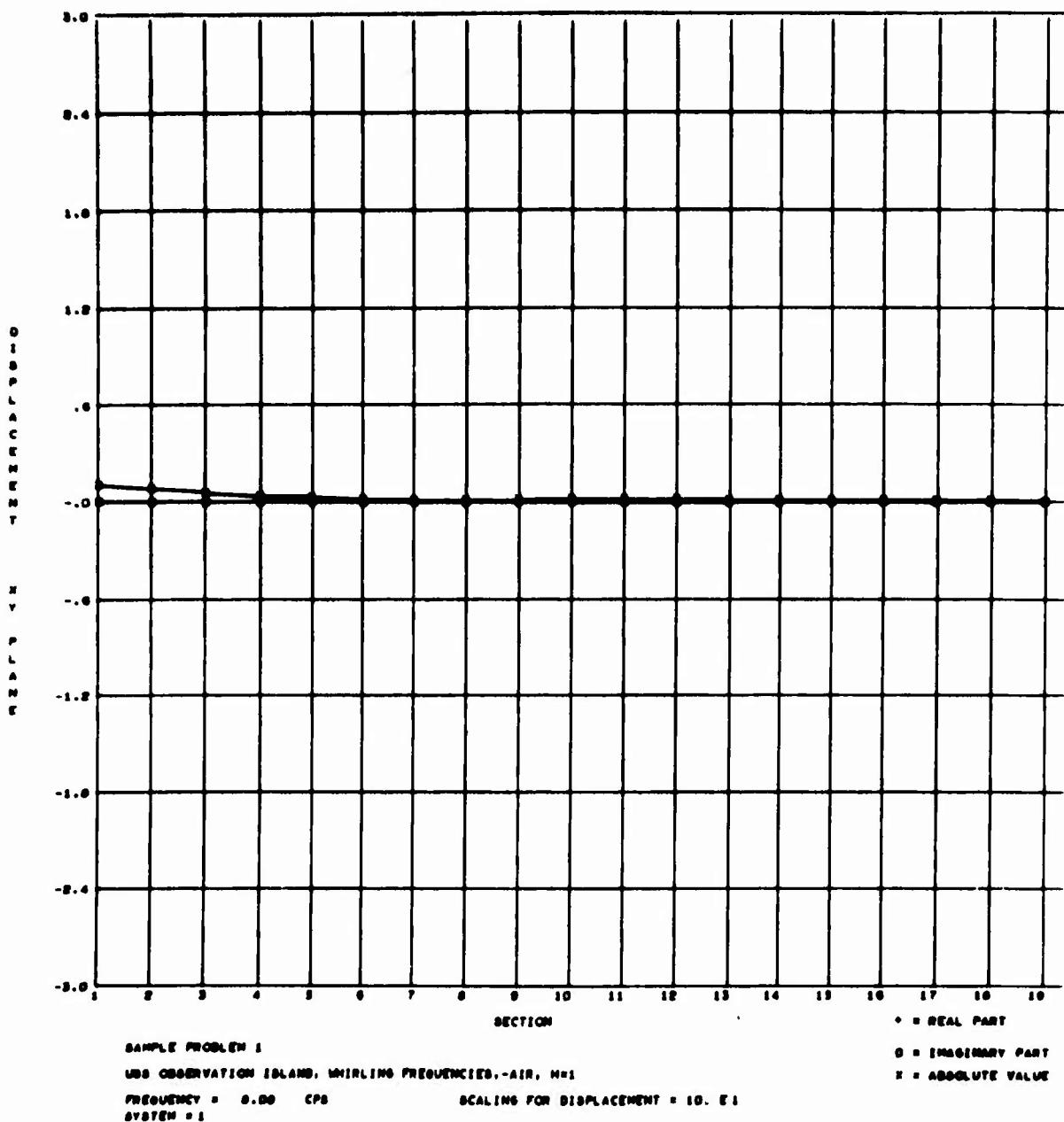
UGG OBSERVATION ISLAND, WHIRLING FREQUENCIES, -AIR, Hz

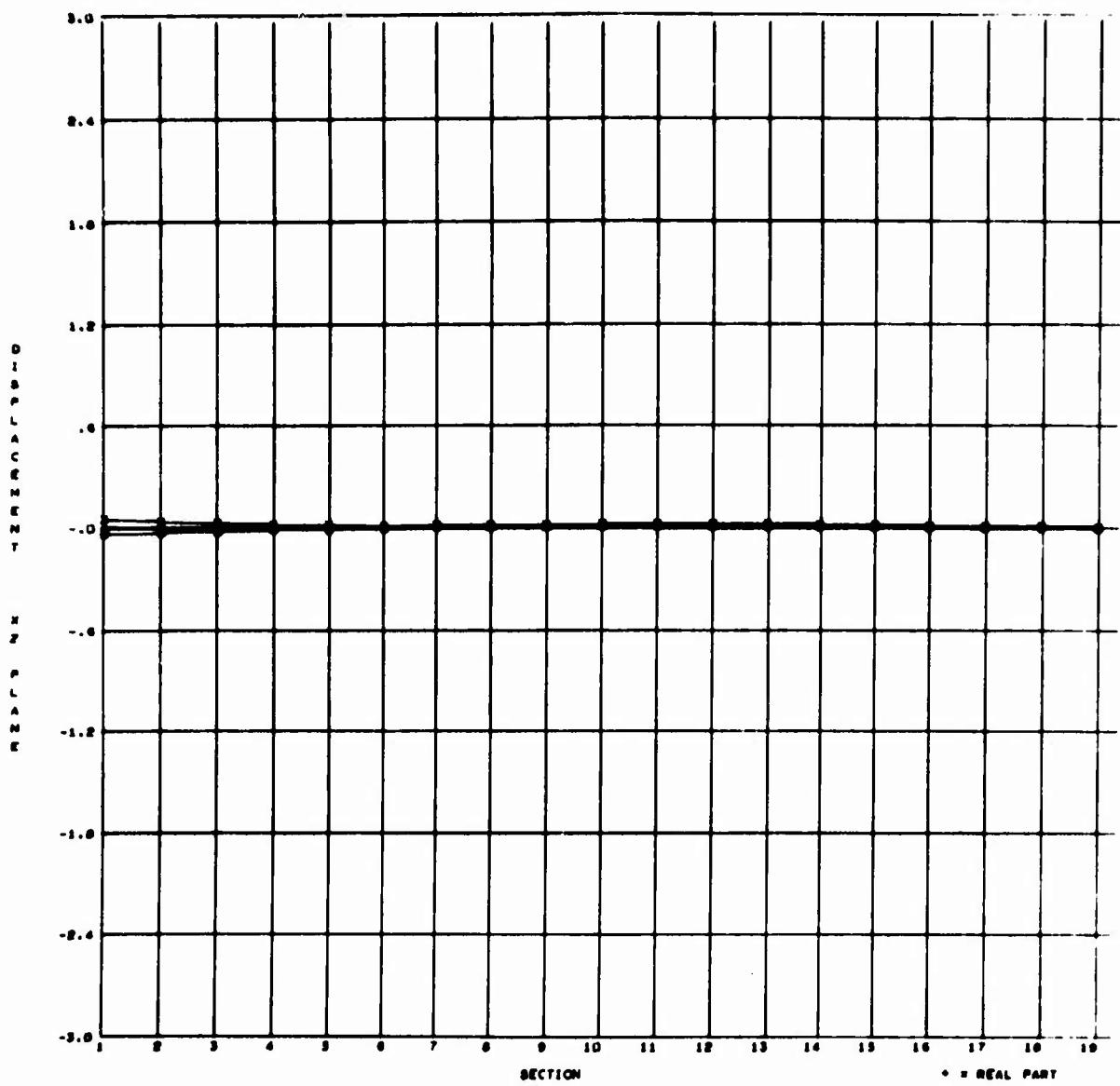
FREQUENCY = 6.37 CPS
SYSTEM = 1

SCALING FOR DISPLACEMENT = 10. E1



6?





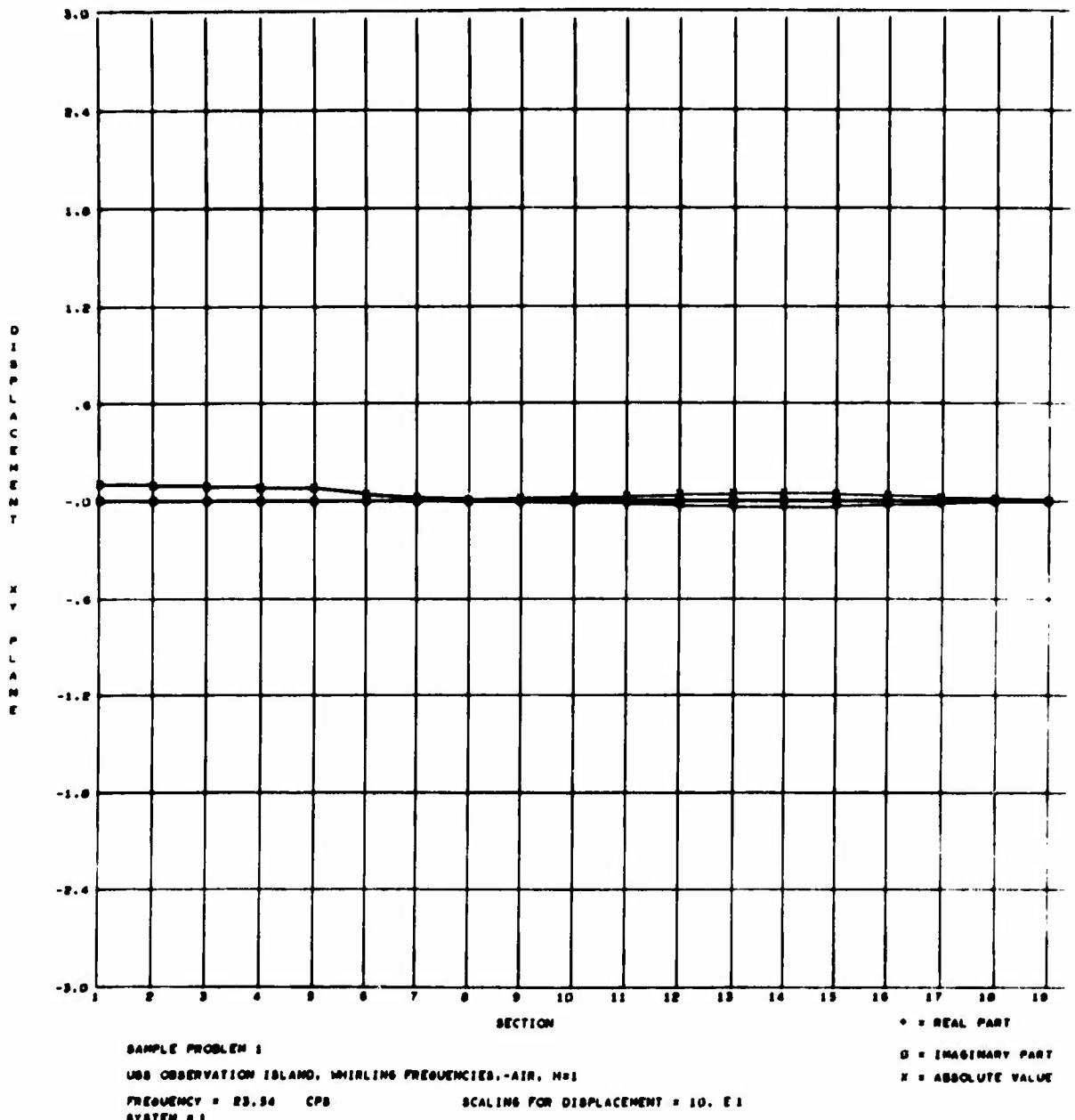
SAMPLE PROBLEM 1

UGG OBSERVATION ISLAND, WHIRLING FREQUENCIES,-AIR, Hz

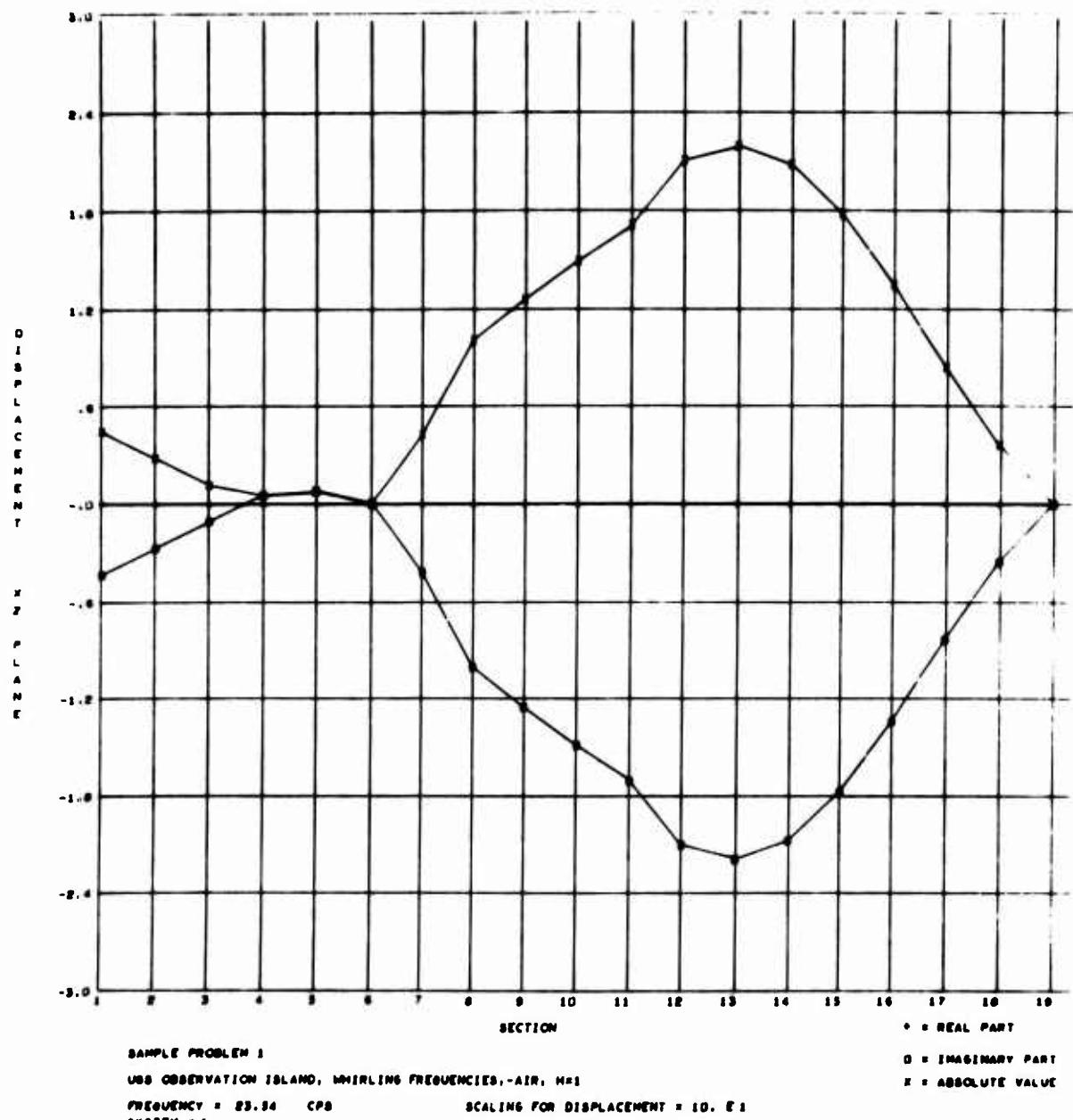
FREQUENCY = 0.00 CPS
SYSTEM = 1

SCALING FOR DISPLACEMENT = 10. E 1

o = IMAGINARY PART
x = ABSOLUTE VALUE



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Problem 2. The data for this calculation is exactly that of Problem 1. except that h is specified as 0.25.

It should be noted that both of these calculations can be done in one running on the computer by using the following sequence of cards after the last card of shaft data for Problem 1.:

1)	00 90 0110 0130
2)	001000(62H ^{AA} TITLE FOR THIS CASE
3)	003000191.0 30.0 1.0 0.25
4)	0099

This affects a saving in computer time since only the case title and values on the type "30" card are restored in memory, all other data remaining as it was in the previous problem.

Since the output presented here is from calculations performed at different stages of the program's testing, it doesn't reflect this facility.

GBRC3 CCT 7. 1966
SAMPLE PROBLEM 2

DATA CONTROL CARD

NO	TYPE
1	10
1	20
1	30
1	41
19	43
2	51
4	53
1	70
1	60

CASE TITLE-USS OBSERVATION ISLAND. WHIRLING FREQUENCIES.-AIR. H=1/4

CPTION DATA
20 -0 2 -0 1 -0 1 -0 -0 -0 1

GENERAL DATA - NUMBER OF SECTIONS 19
WHIRLING FREQUENCY RANGE FROM
FREQUENCY INTERVAL 1.000 CPS
RATIC OF SPIN TO WHIRL = 0.250

REAL PARTS OF SCALING FACTORS

SECTION-END CONDN-SYSTEM	MASS	WATER INERTIA	DX/EI(N)	DX/KAG(N,N+1)	TAUD*DX(N,N+1)	P(N)/Y
1	1.0000E 00	-0.	1.0000E-11	1.0000E 00	1.0000E-09	1.0000E 00
TAU*DX(N,N+1) KA*D(X(N,N+1))	KB*D(X(N,N+1))	P(N)/Z				
1.0000E 05	-0.	1.0000E 09	1.0000E 00			

PARAMETER VALUES FOR EACH SECTION - UNSCALED

SECTION-END CONDN-SYSTEM	MASS	WATER INERTIA	DX/EI(N)	DX/KAG(N,N+1)	TAUD*DX(N,N+1)	P(N)/Y
1 1	5.1900E 01	-0.	1.5310E 01	3.2000E 01	3.2000E-06	5.7860E-03 -0.
TAU*DX(N,N+1) KA*D(X(N,N+1))	KB*D(X(N,N+1))	P(N)/Z				
1.1580E-03	-0.	-0.				
2 0 1	MASS	WATER INERTIA	DX/EI(N)	DX/KAG(N,N+1)	TAUD*DX(N,N+1)	P(N)/Y
5.1900E 01	-0.	1.0000E-15	3.2000E 01	3.2000E-06	7.2350E 00	-0.
TAU*DX(N,N+1) KA*D(X(N,N+1))	KB*D(X(N,N+1))	P(N)/Z				
1.4470E 00	-0.	-0.				
3 0 1	MASS	WATER INERTIA	DX/EI(N)	DX/KAG(N,N+1)	TAUD*DX(N,N+1)	P(N)/Y
5.1900E 01	-0.	1.0000E-15	3.2000E 01	1.9000E-06	7.2350E 00	-0.
TAU*DX(N,N+1) KA*D(X(N,N+1))	KB*D(X(N,N+1))	P(N)/Z				
1.4470E 00	-0.	-0.				

4	0	1	MASS 1.9960E 00	WATER INERTIA -0.	$DX/EI(N)$ 1.2295E 00	$DX/KAG(N,N+1)$ 6.0000E 00	$TAUD*DX(N,N+1)$ 2.2108E 00	$P(N)/Y$ 5.7880E-03	-0.
			$TAU*DX(N,N+1)$ 1.1580E-03	$KA*DX(N,N+1)$ -0.	$KR*DX(N,N+1)$ -0.	$P(N)/Z$			
5	0	1	MASS 1.1640E 01	WATER INERTIA -0.	$DX/EI(N)$ 7.1721E 00	$DX/KAG(N,N+1)$ 3.5000E 01	$TAUD*DX(N,N+1)$ 1.2896E 01	$P(N)/Y$ 1.4910E-02	-0.
			$TAU*DX(N,N+1)$ 2.9820E-03	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -C.	$P(N)/Z$			
6	0	1	MASS 1.1640E 01	WATER INERTIA -0.	$DX/EI(N)$ 7.1721E 00	$DX/KAG(N,N+1)$ 3.5000E 01	$TAUD*DX(N,N+1)$ 1.2896E 01	$P(N)/Y$ 1.4910E-02	-0.
			$TAU*DX(N,N+1)$ 2.9820E-03	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -0.	$P(N)/Z$			
7	0	1	MASS 1.1640E C1	WATER INERTIA -0.	$DX/EI(N)$ 7.1721E 00	$DX/KAG(N,N+1)$ 3.5000E 01	$TAUD*DX(N,N+1)$ 1.2896E 01	$P(N)/Y$ 1.4910E-02	-0.
			$TAU*DX(N,N+1)$ 2.9820E-03	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -0.	$P(N)/Z$			
8	c	1	MASS 4.0900E 00	WATER INERTIA -0.	$DX/EI(N)$ 3.0738E 00	$DX/KAG(N,N+1)$ 1.5000E 01	$TAUD*DX(N,N+1)$ 5.5269E 00	$P(N)/Y$ 2.2330E-02	-0.
			$TAU*DX(N,N+1)$ 4.4660E-03	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -0.	$P(N)/Z$			
9	0	1	MASS 4.9900E C0	WATER INERTIA -0.	$DX/EI(N)$ 3.0738E 00	$DX/KAG(N,N+1)$ 1.5000E 01	$TAUD*DX(N,N+1)$ 5.5269E 00	$P(N)/Y$ 2.2330E-02	-0.
			$TAU*DX(N,N+1)$ 4.4660E-03	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -0.	$P(N)/Z$			
10	0	1	MASS 4.9900E 00	WATER INERTIA -0.	$DX/EI(N)$ 3.0738E 00	$DX/KAG(N,N+1)$ 1.5000E 01	$TAUD*DX(N,N+1)$ 5.5269E 00	$P(N)/Y$ 2.2330E-02	-0.
			$TAU*DX(N,N+1)$ 5.8420E-02	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -0.	$P(N)/Z$			
11	0	1	MASS 1.5000E 01	WATER INERTIA -0.	$DX/EI(N)$ 9.2213E 00	$DX/KAG(N,N+1)$ 4.5000E 01	$TAUD*DX(N,N+1)$ 1.6580E 01	$P(N)/Y$ 2.9210E-01	-0.
			$TAU*DX(N,N+1)$ 5.8420E-02	$KA*DX(N,N+1)$ -0.	$KB*DX(N,N+1)$ -0.	$P(N)/Z$			
12	0	1	MASS 1.0300E 01	WATER INERTIA -0.	$DX/EI(N)$ 6.3525E 00	$DX/KAG(N,N+1)$ 3.1000E 01	$TAUD*DX(N,N+1)$ 1.1422E 01	$P(N)/Y$ 1.0930E-01	-0.

			$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}(N,N+1)$	$\text{P}(N)/Y$
			$1.0300E \quad 01 -0.$	$6.3525E \quad 00$	$3.1000E \quad 01$	$1.1422E \quad 01 \quad 1.0930E-01 -0.$
13	0	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.0300E \quad 01 -0.$	$6.3525E \quad 00$	$3.1000E \quad 01$	$1.1422E \quad 01 \quad 1.0930E-01 -0.$
14	0	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.0300E \quad 01 -0.$	$6.3525E \quad 00$	$3.1000E \quad 01$	$1.1422E \quad 01 \quad 1.0930E-01 -0.$
15	0	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.0300E \quad 01 -0.$	$6.3525E \quad 00$	$3.1000E \quad 01$	$1.1422E \quad 01 \quad 1.0930E-01 -0.$
16	0	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.0300E \quad 01 -0.$	$6.3525E \quad 00$	$3.1000E \quad 01$	$1.1422E \quad 01 \quad 1.0930E-01 -0.$
17	0	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.0300E \quad 01 -0.$	$6.3525E \quad 00$	$3.1000E \quad 01$	$1.1422E \quad 01 \quad 1.0930E-01 -0.$
18	0	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$2.1860E-02 -0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.5000E \quad 01 -0.$	$9.2213E \quad 00$	$-0.$	
19	2	1	$\text{TAU}^{\star}\text{DX}(N,N+1) \text{KA}^{\star}\text{DX}(N,N+1)$	$\text{KB}^{\star}\text{DX}(N,N+1)$	$\text{P}(N)/Z$	
			$-0.$	$-0.$	$-0.$	
			$\text{MASS} \quad \text{WATER INERTIA}$	$\text{DX}/\text{EI}(N)$	$\text{DX}/\text{KAG}(N,N+1)$	$\text{P}(N)/Y$
			$1.0000E \quad 06 -0.$	$-0.$	$-0.$	
			$\text{SYSTEM} \quad \text{C}(N,M)/Y$	$\text{C}(N,M)/W/Y$	$\text{DX}(N,M)$	$\text{Q}(N,M) -0.$
			$1 -0.0000E \quad 06$	$-0.$	$-0.$	
			$\text{TAU}^{\star}\text{DX}(N,M) \text{KA}^{\star}\text{DX}(N,M)$	$\text{KB}^{\star}\text{DX}(N,M)$	$\text{K}(N,M)/Z$	$\text{C}(N,M)/W/Z \quad \text{Q}(N,M)/Z$

REAL PARTS OF SCALING FACTORS

			-0.	-0.	-0.	-0.	1.0000E 09	-0.	-0.	-0.
			K(N.M)/Y	C(N.M)/Y	C(N.M)/W/Y	DX(N.M)	DX/KAG(N.M)	TAUD*DX(N.M)	Q(N.M)/Y	
2	1.0000E 16	-0.	-0.	-0.	-0.	-0.	-0.	-0.	-0.	
			TAU*DX(N.M)	KA*DX(N.M)	K(N.M)/Z	C(N.M)/Z	C(N.M)/W/Z	C(N.M)/Z	-0.	
			-0.	-0.	1.0000E 16	-0.	-0.	-0.	-0.	
PARAMETER VALUES FOR SPECIAL CONNECTIONS										
N	M	SYSTEM	K(N.M)/Y	C(N.M)/Y	C(N.M)/W/Y	DX(N.M)	DX/KAG(N.M)	TAUD*DX(N.M)	Q(N.M)/Y	
6	0	1	9.7030E 00	-0.	-0.	-0.	-0.	-0.	-0.	
			TAU*DX(N.M)	KA*DX(N.M)	K8*DX(N.M)	K(N.M)/Z	C(N.M)/Z	C(N.M)/Z	-0.	
			-0.	-0.	-0.	2.5680E 00	-0.	-0.	-0.	
			K(N.M)/Y	C(N.M)/Y	C(N.M)/W/Y	DX(N.M)	DX/KAG(N.M)	TAUD*DX(N.M)	Q(N.M)/Y	
8	0	1	4.3660E 30	-0.	-0.	-0.	-0.	-0.	-0.	
			TAU*DX(N.4)	KA*DX(N.M)	K8*DX(N.M)	K(N.M)/Z	C(N.M)/Z	C(N.M)/Z	-0.	
			-0.	-0.	-0.	-0.	-0.	-0.	-0.	
			K(N.M)/Y	C(N.M)/Y	C(N.M)/W/Y	DX(N.M)	DX/KAG(N.M)	TAUD*DX(N.M)	Q(N.M)/Y	
1?	0	1	1.3100E 30	-0.	-0.	-0.	-0.	-0.	-0.	
			TAU*DX(N.M)	KA*DX(N.M)	K8*DX(N.M)	K(N.M)/Z	C(N.M)/Z	C(N.M)/Z	-0.	
			-0.	-0.	-0.	-0.	-0.	-0.	-0.	
			K(N.M)/Y	C(N.M)/Y	C(N.M)/W/Y	DX(N.M)	DX/KAG(N.M)	TAUD*DX(N.M)	Q(N.M)/Y	
19	0	2	1.0000E 00	-0.	-0.	-0.	-0.	-0.	-0.	
			TAU*DX(N.M)	KA*DX(N.M)	K8*DX(N.M)	K(N.M)/Z	C(N.M)/Z	C(N.M)/Z	-0.	
			-0.	-0.	1.0000E 00	-0.	-0.	-0.	-0.	

NFREC = 3
CHAR(1)= ♦
CHAR(2)= ♦
CHAR(3)= O
CHAR(4)= X
CHAR(5)= -
CHAR(6)= *

GBRC3

SAMPLE PROBLEM 2

USS OBSERVATION ISLAND. WHIRLING FREQUENCIES.-AIR. H=1/4

FREQUENCY 6.50 CPS

XY-PLANE

SECTION	DEFLECTIONS			MOMENTS		
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART
1	1.0000E 00	0*	1.0000E 00	0.	7.4553E-06	-0*
2	7.6143E-01	-0*	7.6143E-01	-0*	-2.8729E 06	0*
3	5.2286E-01	-0*	5.2286E-01	-0*	-1.3959E 07	0*
4	2.8429E-01	0*	2.8429E-01	0*	-2.6495E 07	0*
5	2.4106E-01	0*	2.4106E-01	0*	-2.7711E 07	0*
6	5.8424E-02	0*	5.8424E-02	0*	-3.4950E 07	0*
7	-2.9187E-02	-0*	2.9187E-02	*	-2.2384E 07	0*
8	-6.0601E-02	-0*	6.0601E-02	*	-9.7963E 06	0*
9	-7.1006E-02	-0*	7.1006E-02	*	-8.3660E 06	0*
10	-7.7551E-02	-0*	7.7551E-02	*	-6.9255E 06	0*
11	-8.0900E-02	-0*	8.0900E-02	*	-5.4742E 06	0*
12	-6.8196E-02	-0*	6.8196E-02	*	-1.0156E 06	0*
13	-5.8451E-02	-0*	5.8451E-02	*	-6.7107E 05	0*
14	-4.7374E-02	-0*	4.7374E-02	*	-2.8970E 05	0*
15	-3.5716E-02	-0*	3.5716E-02	*	-1.2056E 05	0*
16	-2.4289E-02	-0*	2.4289E-02	*	5.5134E 05	0*
17	-1.3943E-02	-0*	1.3943E-02	*	9.9430E 05	0*
18	-5.5527E-03	-0*	5.5527E-03	*	1.4416E 06	0*
19	-1.3992E-12	-0*	1.3992E-12	*	1.8866E 06	0*

XZ-PLANE

SECTION	DEFLECTIONS			MOMENTS		
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART
1	-0*	1.1274E 01	1.1274E 01	9.0000E 01	-0*	8.6213E-05
2	-0*	8.5156E 00	8.5156E 00	9.0000E 01	-0*	-3.1269E 07
3	-0*	5.7568E 00	5.7568E 00	9.0000E 01	-0*	-9.7003E 07
4	-0*	2.9980E 00	2.9980E 00	9.0000E 01	-0*	-1.7870E 08
5	-0*	2.4889E 00	2.4889E 00	9.0000E 01	-0*	-1.9205E 08
6	0*	1.1929E-03	1.1929E-03	9.0000E 01	-0*	-2.7158E 08
7	0*	-1.7653E 00	1.7653E 00	-9.0000E 01	-0*	-2.4399E 08
8	0*	-2.9192E 00	2.9192E 00	-9.0000E 01	-0*	-2.1500E 08
9	0*	-3.3144E 00	3.3144E 00	-9.0000E 01	-0*	-2.0226E 08
10	0*	-3.6162E 00	3.6162E 00	-9.0000E 01	-0*	-1.8911E 08
11	0*	-3.6307E 00	3.6307E 00	-9.0000E 01	-0*	-1.7549E 08
12	0*	-3.7443E 00	3.7443E 00	-9.0000E 01	-0*	-1.3032E 08
13	0*	-3.4274E 00	3.4274E 00	-9.0000E 01	-0*	-9.7191E 07
14	0*	-2.9184E 00	2.9184E 00	-9.0000E 01	-0*	-6.2224E 07
15	0*	-2.2863E 00	2.2863E 00	-9.0000E 01	-0*	-2.5693E 07
16	0*	-1.16032E 00	1.16032E 00	-9.0000E 01	-0*	-1.2059E 07
17	0*	-9.4351E-01	9.4351E-01	-9.0000E 01	-0*	5.0664E 07
18	0*	-3.8341E-01	3.8341E-01	-9.0000E 01	-0*	8.9766E 07
19	0*	-1.26669E-10	1.26669E-10	-9.0000E 01	-0*	1.2906E 08

GBRC3

SAMPLE PROBLEM 2

USS OBSERVATION ISLAND. WHIRLING FREQUENCIES.-AIR. H=1/4

FREQUENCY

7.84 CPS

XY-PLANE

SECTION	DEFLECTIONS					REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART								
1	1.0000E 00	0*	1.0000E 00	0*	7.3091E-06	-0.		7.3091E-06	-0.			7.3091E-06	-0.
2	7.6611E-01	-0*	7.6611E-01	-0*	-4.0372E 06	-0.		-4.0372E 06	-0.			4.0372E 06	0.
3	5.3222E-01	-0*	5.3222E-01	-0*	-1.2372E 07	-0.		-1.2372E 07	-0.			1.2372E 07	0.
4	2.9833E-01	0*	2.9833E-01	0*	-2.2854E 07	-0.		-2.2854E 07	-0.			2.2854E 07	0.
5	2.5551E-01	0*	2.5551E-01	0*	-2.4602E 07	-0.		-2.4602E 07	-0.			2.4602E 07	0.
6	6.7434E-02	0*	6.7434E-02	0*	-3.5052E 07	-0.		-3.5052E 07	-0.			3.5052E 07	0.
7	-2.4243E-02	-0*	2.4243E-02	-0*	-2.2667E 07	-0.		-2.2667E 07	-0.			2.2667E 07	0.
8	-5.9013E-02	-0*	5.9013E-02	-0*	-1.0257E 07	-0.		-1.0257E 07	-0.			1.0257E 07	0.
9	-7.0604E-02	-0*	7.0604E-02	-0*	-8.7927E 06	-0.		-8.7927E 06	-0.			8.7927E 06	0.
10	-7.8137E-02	-0*	7.8137E-02	-0*	-7.3155E 06	-0.		-7.3155E 06	-0.			7.3155E 06	0.
11	-8.2292E-02	-0*	8.2292E-02	-0*	-5.8239E 06	-0.		-5.8239E 06	-0.			5.8239E 06	0.
12	-7.0541E-02	-0*	7.0541E-02	-0*	-1.2123E 06	-0.		-1.2123E 06	-0.			1.2123E 06	0.
13	-6.1093E-02	-0*	6.1093E-02	-0*	-8.4575E 05	-0.		-8.4575E 05	-0.			8.4575E 05	0.
14	-4.9962E-02	-0*	4.9962E-02	-0*	-4.3177E 05	-0.		-4.3177E 05	-0.			4.3177E 05	0.
15	-3.7967E-02	-0*	3.7967E-02	-0*	-2.0989E 04	-0.		-2.0989E 04	-0.			2.0989E 04	0.
16	-2.6002E-02	-0*	2.6002E-02	-0*	-5.0317E 05	-0.		-5.0317E 05	-0.			5.0317E 05	0.
17	-1.5021E-02	-0*	1.5021E-02	-0*	-1.0054E 06	-0.		-1.0054E 06	-0.			1.0054E 06	0.
18	-6.0152E-03	-0*	6.0152E-03	-0*	-1.5192E 06	-0.		-1.5192E 06	-0.			1.5192E 06	0.
19	-1.6709E-12	-0*	1.6709E-12	-0*	-2.0375E 06	-0.		-2.0375E 06	-0.			2.0375E 06	0.

XZ-PLANE

SECTION	DEFLECTIONS					REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE
	REAL PART	IMAG PART	ABS VALUE	PHASE ANGLE	REAL PART								
1	0*	1.1684E-01	1.1684E-01	-9.0000E 01	0*	-8.6340E-07	8.8330E-07	-8.6340E-07	-9.0000E 01				
2	0*	8.8573E-02	8.8573E-02	-9.0000E 01	0*	4.7105E 05	4.7105E 05	4.7105E 05	9.0000E 01				
3	0*	-6.0304E-02	6.0304E-02	-9.0000E 01	0*	8.1279E 05	8.1279E 05	8.1279E 05	9.0000E 01				
4	0*	-3.2035E-02	3.2035E-02	-9.0000E 01	0*	1.3978E 06	1.3978E 06	1.3978E 06	9.0000E 01				
5	0*	-2.6763E-02	2.6763E-02	-9.0000E 01	0*	1.5994E 06	1.5994E 06	1.5994E 06	9.0000E 01				
6	0*	-1.6109E-05	1.6109E-05	-9.0000E 01	0*	2.8033E 06	2.8033E 06	2.8033E 06	9.0000E 01				
7	-1.9160E-02	1.9160E-02	9.0000E 01	0*	-2.5598E 06	2.5598E 06	2.5598E 06	9.0000E 01					
8	-3.1904E-02	3.1904E-02	9.0000E 01	0*	-2.2975E 06	2.2975E 06	2.2975E 06	9.0000E 01					
9	-3.6304E-02	3.6304E-02	9.0000E 01	0*	-2.1793E 06	2.1793E 06	2.1793E 06	9.0000E 01					
10	-3.9697E-02	3.9697E-02	9.0000E 01	0*	-2.0545E 06	2.0545E 06	2.0545E 06	9.0000E 01					
11	-4.2140E-02	4.2140E-02	9.0000E 01	0*	-1.9225E 06	1.9225E 06	1.9225E 06	9.0000E 01					
12	-4.1466E-02	4.1466E-02	9.0000E 01	0*	-1.4581E 06	1.4581E 06	1.4581E 06	9.0000E 01					
13	-3.8118E-02	3.8118E-02	9.0000E 01	0*	-1.1057E 06	1.1057E 06	1.1057E 06	9.0000E 01					
14	-3.2583E-02	3.2583E-02	9.0000E 01	0*	-7.62354E 05	7.62354E 05	7.62354E 05	9.0000E 01					
15	-2.5613E-02	2.5613E-02	9.0000E 01	0*	-3.1605E 05	3.1605E 05	3.1605E 05	9.0000E 01					
16	-1.8013E-02	1.8013E-02	9.0000E 01	0*	-1.1136E 05	1.1136E 05	1.1136E 05	-9.0000E 01					
17	-1.0627E-02	1.0627E-02	9.0000E 01	0*	-5.5277E 05	5.5277E 05	5.5277E 05	-9.0000E 01					
18	-4.3227E-03	4.3227E-03	9.0000E 01	0*	-1.0024E 06	1.0024E 06	1.0024E 06	-9.0000E 01					
19	-1.408E-12	1.408E-12	9.0000E 01	0*	-1.4554E 06	1.4554E 06	1.4554E 06	-9.0000E 01					

GBRC3

SAMPLE PROBLEM 2

USS OBSERVATION ISLAND. WHIRLING FREQUENCIES,-AIR. H=1/4

FREQUENCY 23.53 CPS

XY-PLANE

SECTION	DEFLECTIONS			REAL PART	IMAG PART	ABS VALUE	PHASE	ANGLE	REAL PART	IMAG PART	ABS VALUE	PHASE	ANGLE
	REAL PART	IMAG PART	ABS VALUE										
1	1.0000E 00	0*	1.0000E 00	0*		-4.6079E-07	-0*		4.6079E-07	0*			
2	1.0147E 00	-0*	1.0147E 00	-0*		-7.3702E 07	-0*		7.3702E 07	0*			
3	1.0295E 00	-0*	1.0295E 00	-0*		6.5737E 07	0*		6.5737E 07	0*			
4	1.0442E 00	0*	1.0442E 00	0*		1.6779E 08	0*		1.6779E 08	0*			
5	1.0243E 00	0*	1.0243E 00	0*		1.3990E 08	0*		1.3990E 08	0*			
C	5.5339E-01	0*	5.5339E-01	0*		-3.3151E 07	0*		3.3151E 07	0*			
7	2.3313E-01	0*	2.3313E-01	0*		-2.4091E 07	0*		2.4091E 07	0*			
8	-2.7416E-02	-0*	2.7416E-02	-0*		-1.7550E 07	0*		1.7550E 07	0*			
9	-1.3163E-01	-0*	1.3163E-01	-0*		-1.0264E 07	0*		1.0264E 07	0*			
10	-2.2735E-01	-0*	2.2735E-01	-0*		-1.8666E 07	0*		1.8666E 07	0*			
11	-3.1432E-01	-0*	3.1432E-01	-0*		-1.8499E 07	0*		1.8499E 07	0*			
12	-4.9677E-01	-0*	4.9677E-01	-0*		-2.4081E 07	0*		2.4081E 07	0*			
13	-5.8118E-01	-0*	5.8118E-01	-0*		-3.4797E 07	0*		3.4797E 07	0*			
14	-5.9558E-01	-0*	5.9558E-01	-0*		-3.6707E 07	0*		3.6707E 07	0*			
15	-5.3616E-01	-0*	5.3616E-01	-0*		-3.0110E 07	-0*		3.0110E 07	-0*			
16	-4.1606E-01	-0*	4.1606E-01	-0*		-1.6527E 07	-0*		1.6527E 07	-0*			
17	-2.6235E-01	0*	2.6235E-01	0*		1.4953E 06	0*		1.4953E 06	0*			
18	-1.1091E-01	0*	1.1091E-01	0*		2.0724E 07	0*		2.0724E 07	0*			
19	-2.8399E-11	-0*	2.8399E-11	-0*		3.7665E 07	0*		3.7665E 07	0*			

XZ-PLANE

SECTION	DEFLECTIONS			REAL PART	IMAG PART	ABS VALUE	PHASE	ANGLE	REAL PART	IMAG PART	ABS VALUE	PHASE	ANGLE
	REAL PART	IMAG PART	ABS VALUE										
1	0*	-2.6959E 01	2.6959E 01	-9.0000E 01	0*	-3.1528E-04	-9.0000E 01		3.1528E-04	-9.0000E 01			
2	0*	-1.6867E 01	1.6867E 01	-9.0000E 01	0*	9.7940E 08	9.7940E 08	9.0000E 01	9.7940E 08	9.0000E 01			
3	0*	-6.7749E 00	6.7749E 00	-9.0000E 01	-0*	3.0702E 09	3.0702E 09	9.0000E 01	3.0702E 09	9.0000E 01			
4	-0*	-3.3174E 00	3.3174E 00	9.0000E 01	-0*	5.4070E 09	5.4070E 09	9.0000E 01	5.4070E 09	9.0000E 01			
5	-0*	4.9374E 00	4.9374E 00	9.0000E 01	-0*	5.7510E 09	5.7510E 09	9.0000E 01	5.7510E 09	9.0000E 01			
6	0*	-6.4890E-02	6.4890E-02	-9.0000E 01	-0*	7.7112E 09	7.7112E 09	9.0000E 01	7.7112E 09	9.0000E 01			
7	0*	-2.6573E 01	2.6573E 01	-9.0000E 01	-0*	3.8379E 09	3.8379E 09	9.0000E 01	3.8379E 09	9.0000E 01			
8	0*	-6.2628E 01	6.2628E 01	-9.0000E 01	-0*	2.0037E 08	2.0037E 08	9.0000E 01	2.0037E 08	9.0000E 01			
9	0*	-7.8135E 01	7.8135E 01	-9.0000E 01	0*	-1.2596E 09	1.2596E 09	-9.0000E 01	1.2596E 09	-9.0000E 01			
10	0*	-9.3013E 01	9.3013E 01	-9.0000E 01	0*	-2.5914E 09	2.5914E 09	-9.0000E 01	2.5914E 09	-9.0000E 01			
11	0*	-1.0664E 02	1.0664E 02	-9.0000E 01	0*	-3.7707E 09	3.7707E 09	-9.0000E 01	3.7707E 09	-9.0000E 01			
12	0*	-1.3130E 02	1.3130E 02	-9.0000E 01	-0*	-5.7557E 09	5.7557E 09	-9.0000E 01	5.7557E 09	-9.0000E 01			
13	0*	-1.3661E 02	1.3661E 02	-9.0000E 01	-0*	-6.1870E 09	6.1870E 09	-9.0000E 01	6.1870E 09	-9.0000E 01			
14	0*	-1.2939E 02	1.2939E 02	-9.0000E 01	-0*	-5.6551E 09	5.6551E 09	-9.0000E 01	5.6551E 09	-9.0000E 01			
15	0*	-1.1070E 02	1.1070E 02	-9.0000E 01	-0*	-4.2112E 09	4.2112E 09	-9.0000E 01	4.2112E 09	-9.0000E 01			
16	0*	-8.3429E 01	8.3429E 01	-9.0000E 01	-0*	-1.9881E 09	1.9881E 09	-9.0000E 01	1.9881E 09	-9.0000E 01			
17	0*	-5.2030E 01	5.2030E 01	-9.0000E 01	-0*	-8.2055E 08	8.2055E 08	-9.0000E 01	8.2055E 08	-9.0000E 01			
18	0*	-2.2114E 01	2.2114E 01	-9.0000E 01	-0*	-3.9912E 09	3.9912E 09	-9.0000E 01	3.9912E 09	-9.0000E 01			
19	0*	-1.0654E-08	1.0654E-08	-9.0000E 01	-0*	7.3101E 09	7.3101E 09	-9.0000E 01	7.3101E 09	-9.0000E 01			

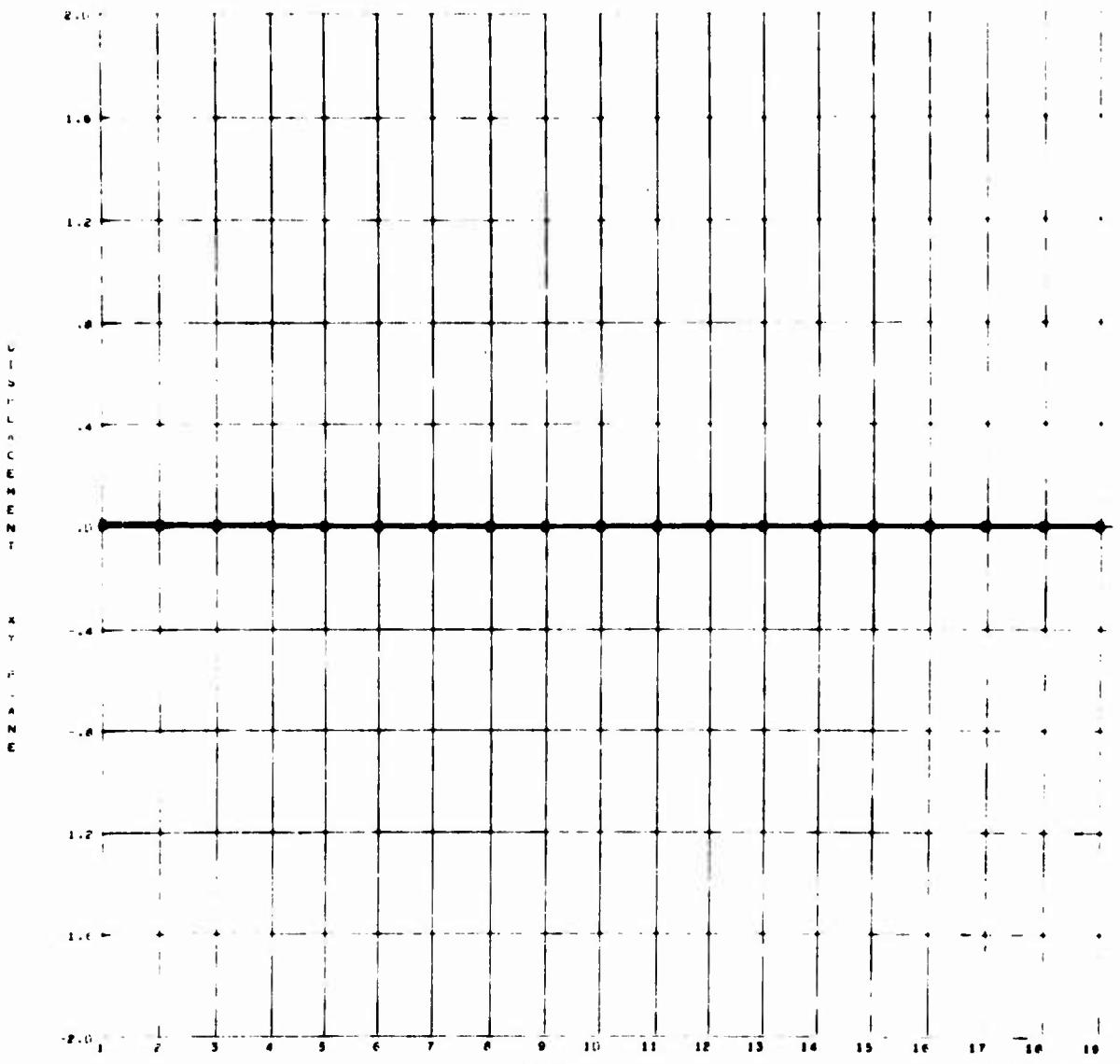
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SAMPLE PROBLEM 2

DATA CONTROL CARD

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END GBRC3 RUN

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SAMPLE PROBLEM 2

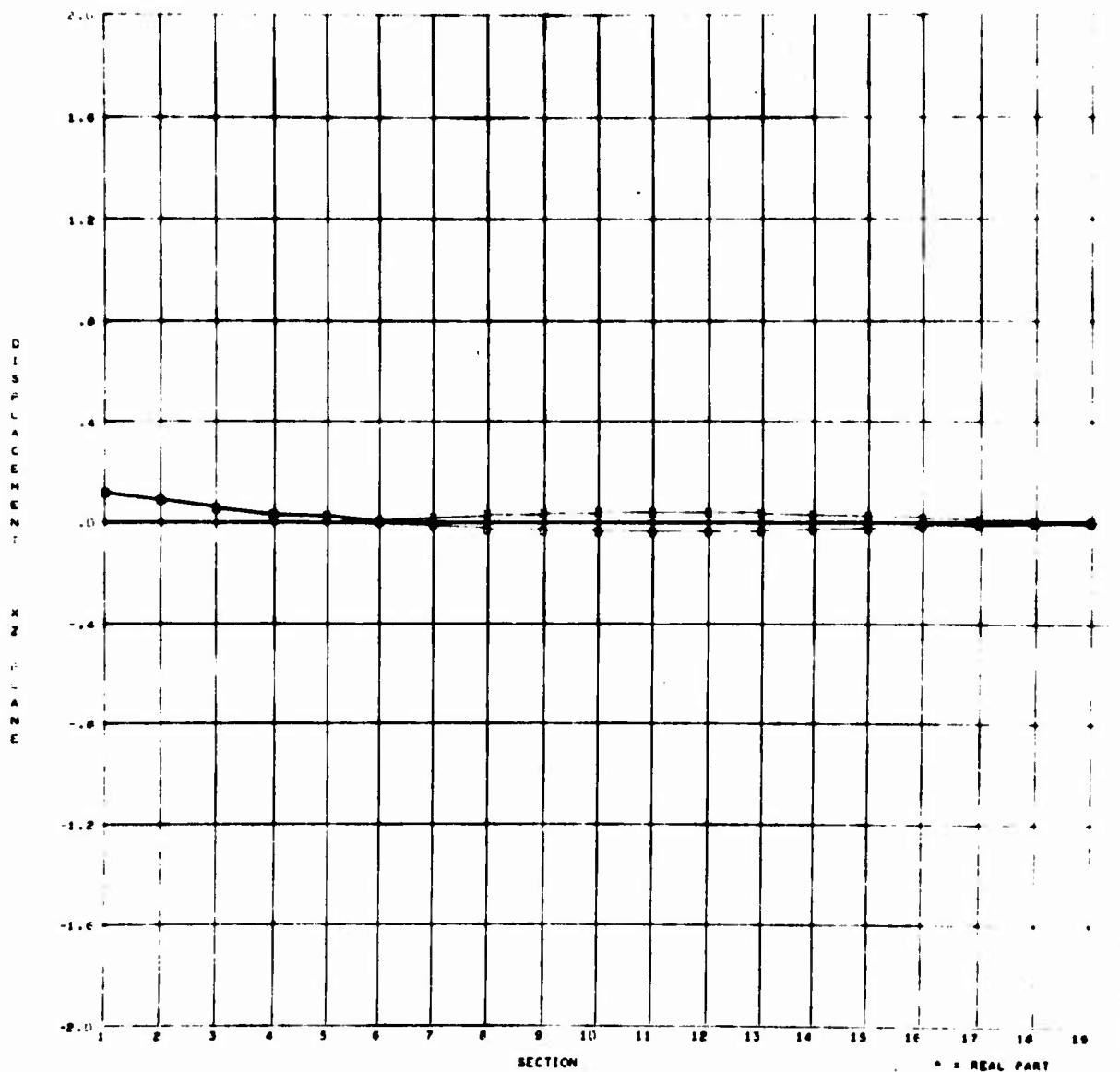
U.S. OBSERVATION ISLAND, WHIRLING FREQUENCIES, AIR, H=1/4

FREQUENCY = 6.50 CFS
SYSTEM = I

SCALING FOR DISPLACEMENT = 10. E2

82

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SAMPLE PROBLEM 2

USS OBSERVATION ISLAND, WHIRLING FREQUENCIES,-AIR, H=1/4

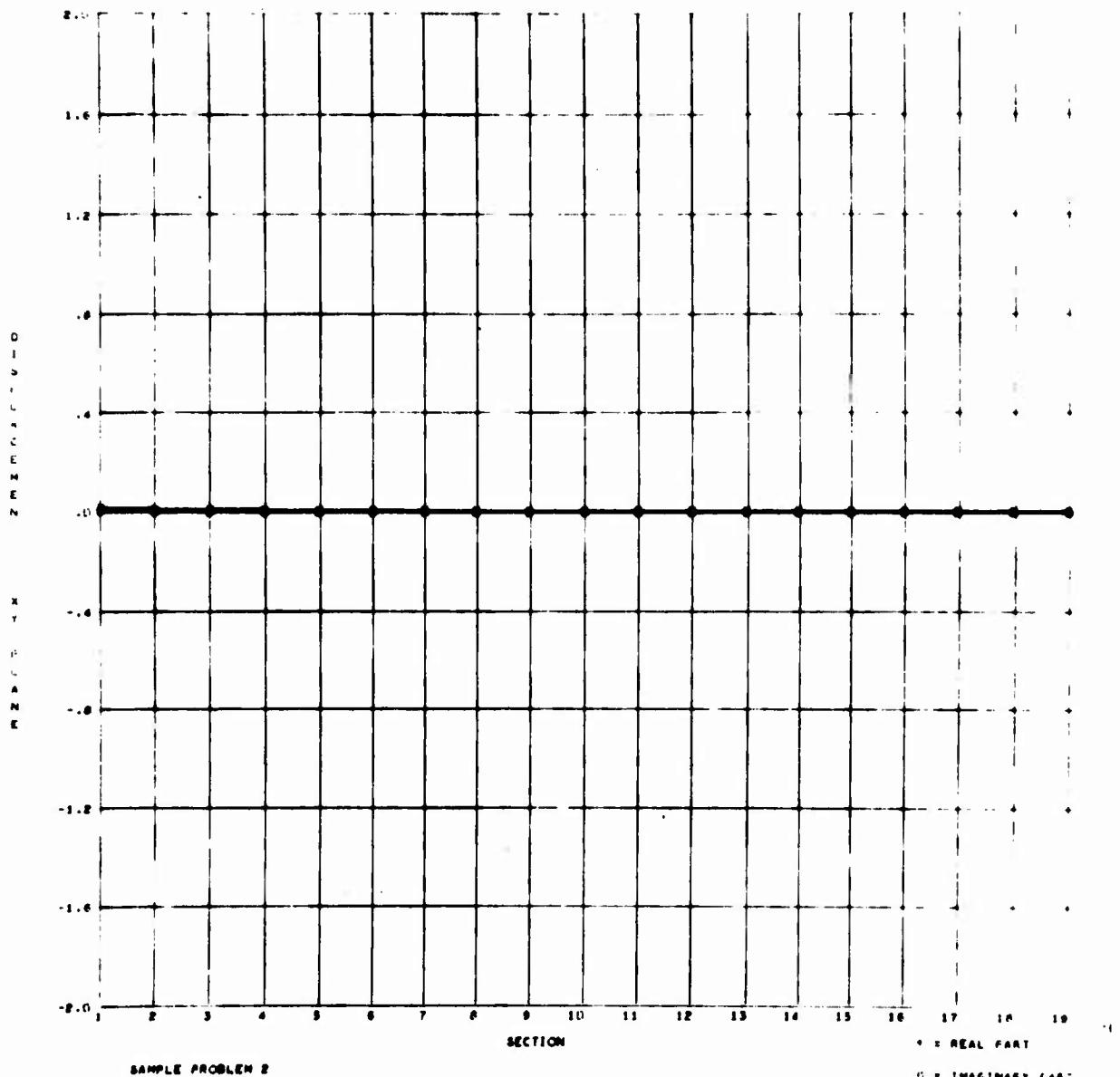
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SYSTEM : I

SCALING FOR DISPLACEMENT = 10. E.P.

- \bullet = REAL PART
- i = IMAGINARY PART
- $\|\cdot\|$ = ABSOLUTE VALUE

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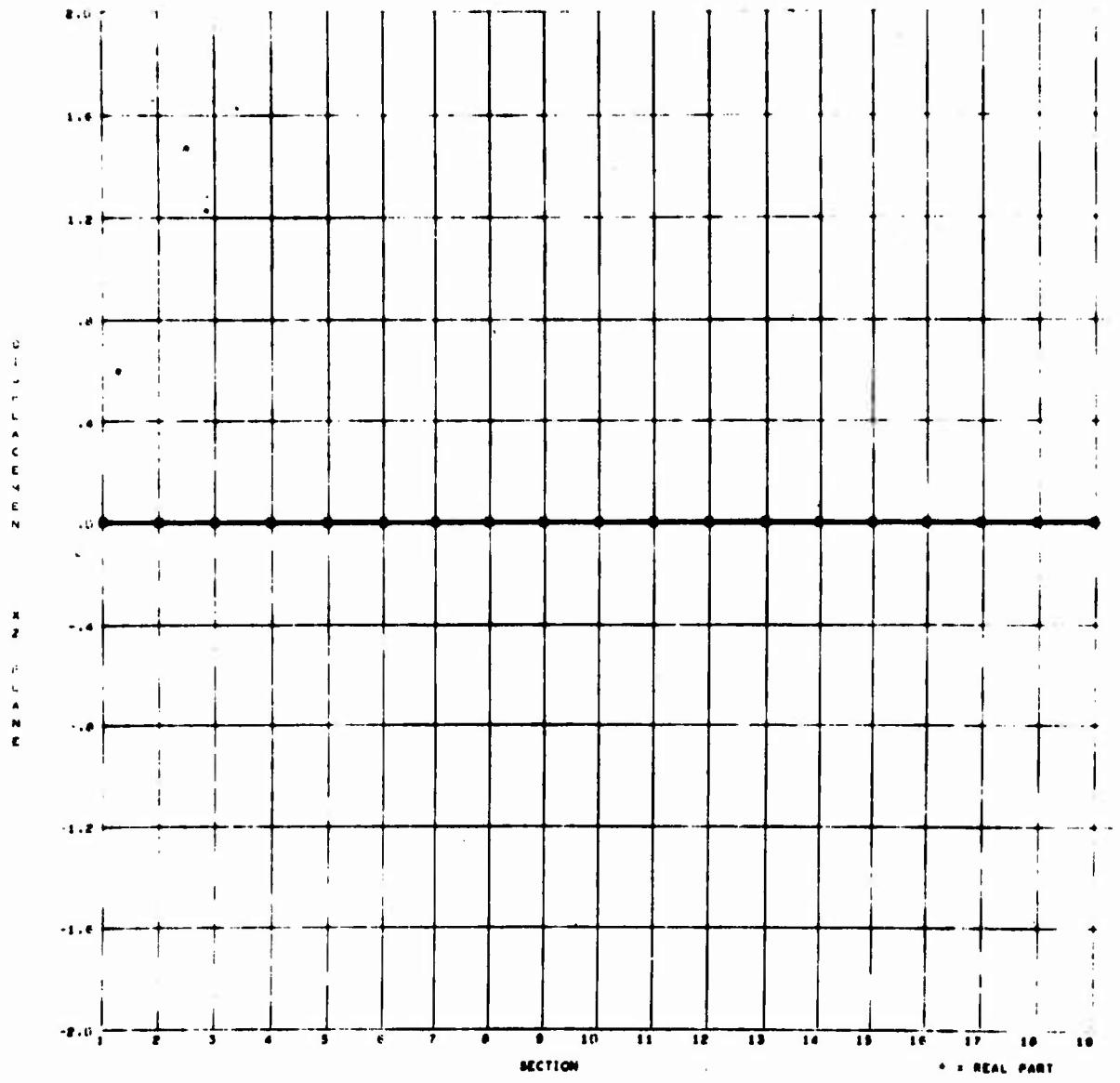
UBB OBSERVATION ISLAND, WHIRLING FREQUENCIES, -AIR, M=1/4

FREQUENCY = 7.06 CPS
SYSTEM 1/1

SCALING FOR DISPLACEMENT = 10. EZ

89

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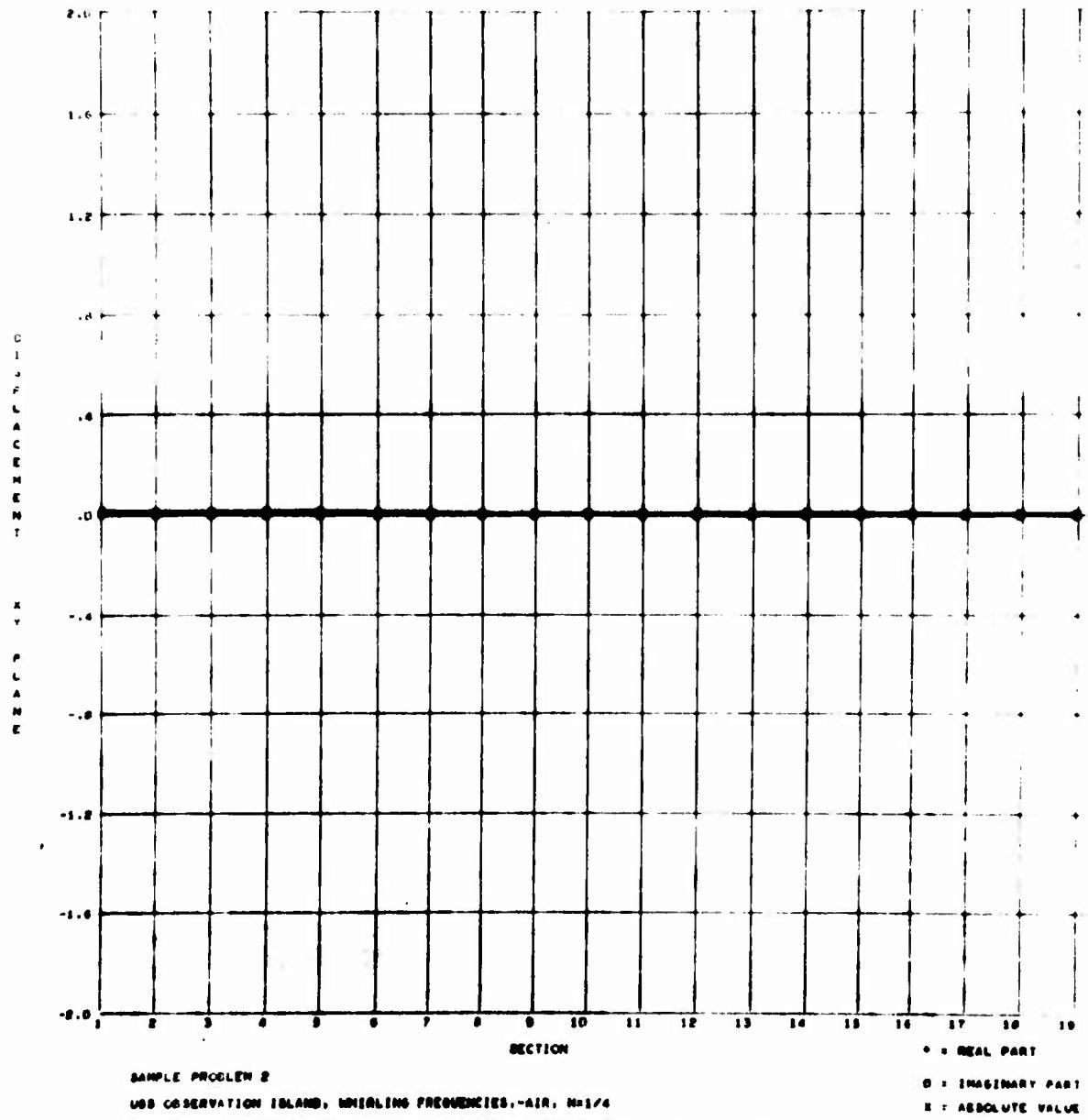
SAMPLE PROBLEM 2

USS OBSERVATION ISLAND, WHIRLING FREQUENCIES, -AIR, M=1/4

FREQUENCY = 7.04 CFS
SYSTEM # 1

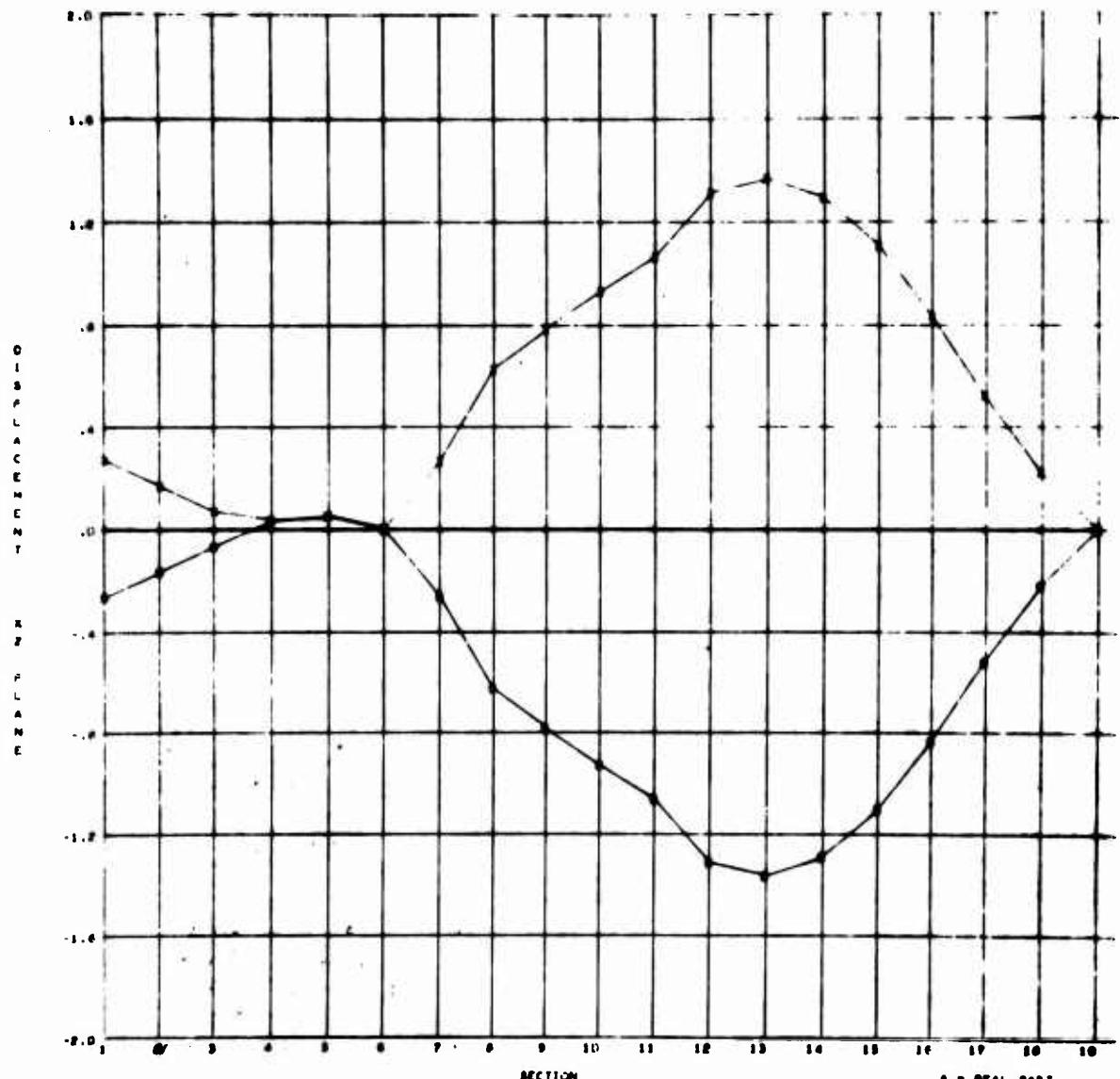
SCALING FOR DISPLACEMENT = 10. E2

85
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USS OBSERVATION ISLAND, WHIRLING FREQUENCIES, AIR, Hz/4

FREQUENCY = 23.53 CPS

SYSTEM = 1

SCALING FOR DISPLACEMENT = 10. E2

87

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TABLE 1

Comparison of Calculated Results

	Mode Number	Critical Whirling Frequencies in CPS	
		AML Computer Program 170	GBRC3*
Problem 1 $h = 1$	1	6.37	6.37
	2	8.08	8.08
	3	23.55	23.54
Problem 2 $h = \frac{1}{4}$	1	6.50	6.50
	2	7.85	7.84
	3	23.55	23.53

* IBM 709 computer running time for each of these problems
is approximately 8 minutes.

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4. Teng, E. C., "General Bending Response Program: GBRP," Applied Mathematics Laboratory Technical Note AML-35-67 (July 1967).

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